

# Do we really need dark matter?— From perspective of MOND

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# Outlines

Background

Clues for dark matter

MOND—the alternative  
to dark matter

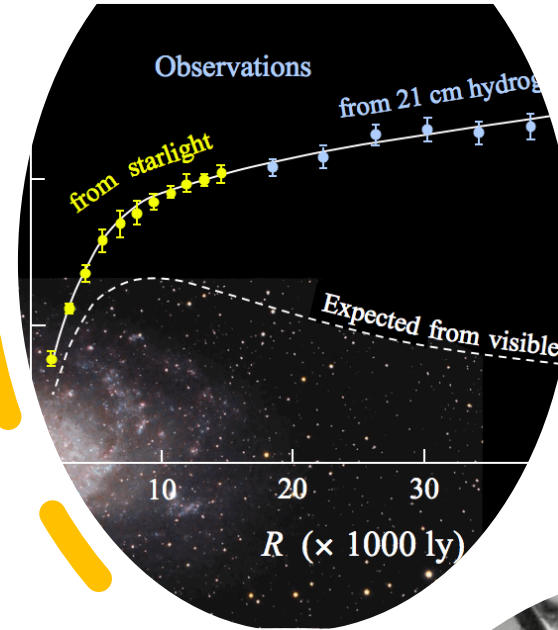
Discussion

# Background

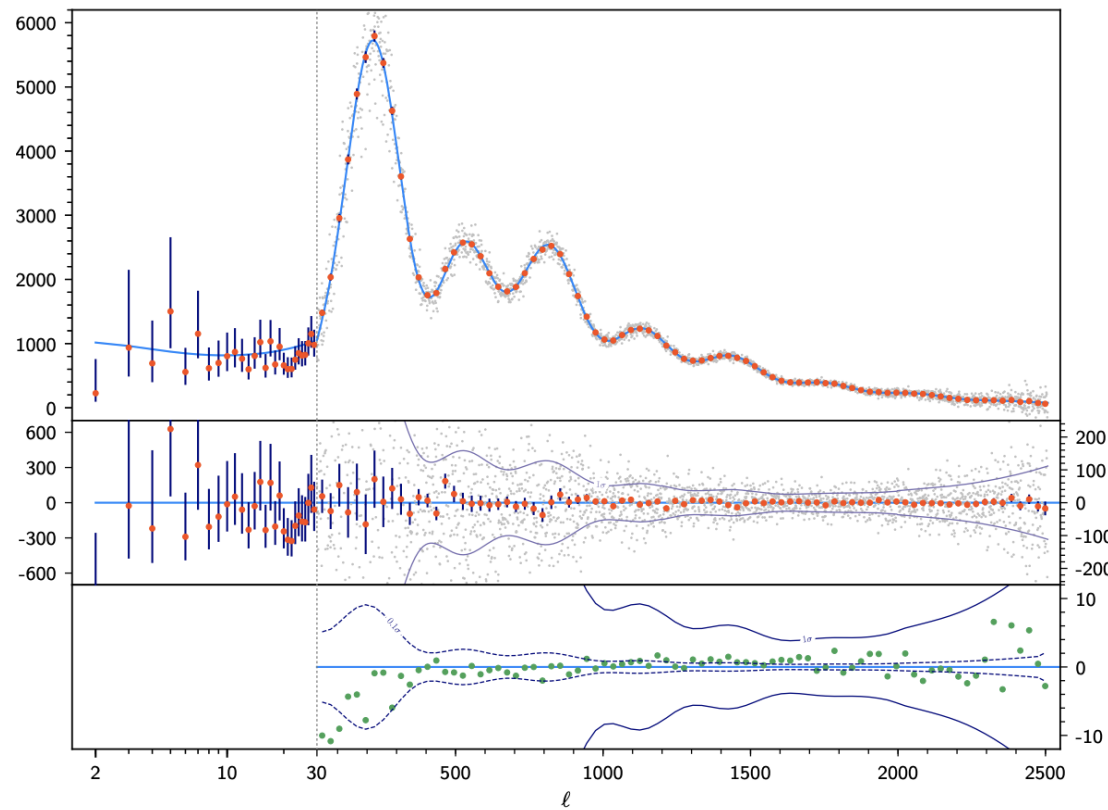
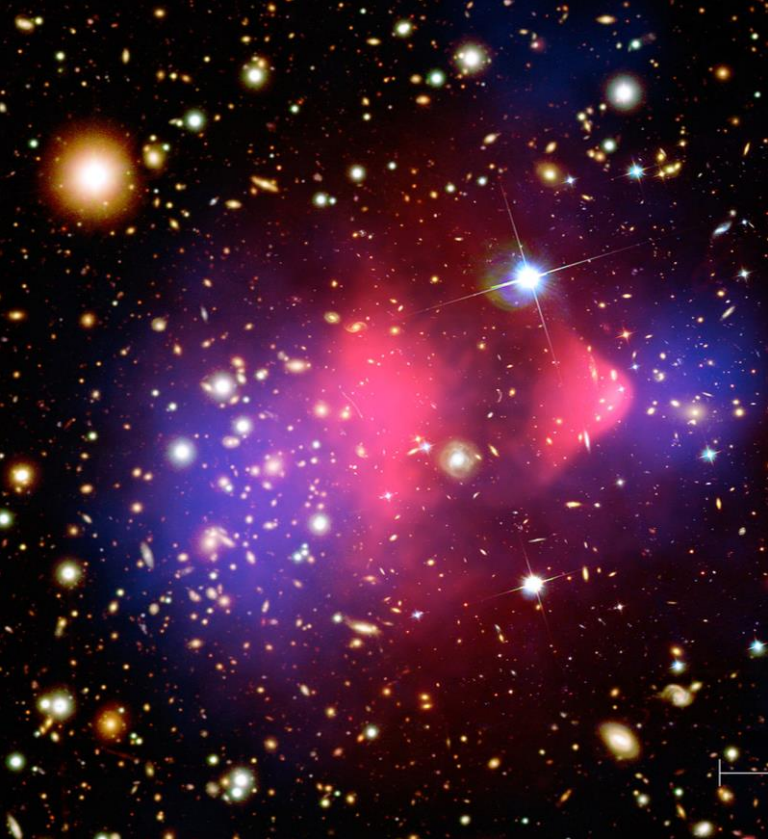
Two interpretations:

- ◆ There are large quantities of **unseen matter**
- ◆ Newton's Laws **do not** apply to galaxies

21 cm line

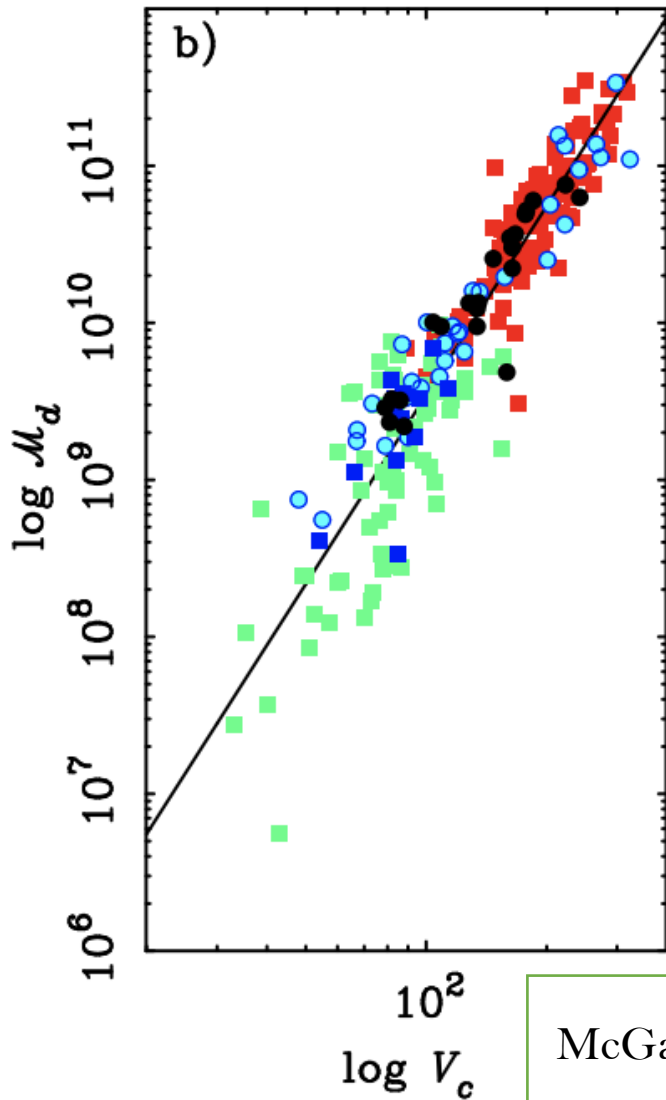


Vera Rubin



## Clues for DM paradigm

- Velocity dispersions
- Galaxy clusters
- Gravitational lensing
- CMB
- Structure formation



McGaugh (2000)

# MOND— alternative to DM

- In 1983, Milgrom developed an *ad hoc* empirical theory to explain the observations in galaxies

- $\mu(|\vec{a}|/a_0)\vec{a} = -\nabla\Phi_N$

with  $\begin{cases} \mu(x) \approx 1 & x \gg 1 \\ \mu(x) \approx x & x \ll 1 \end{cases}$

- Two direct result:

- ◆ In  $x \ll 1$  regime, it reproduce **flat rotation curve**

$$v_c = (GMa_0)^{1/4}$$

- ◆ Baryonic **Tully-Fisher relation**

$$M = (Ga_0)^{-1}v_c^4$$

# Corrections to original MOND

- This simple theory does not conserve momentum
- Using Lagrangian or action

$$\mathcal{L} = -\frac{a_0^2}{8\pi G} f\left(\frac{|\nabla\Phi|^2}{a_0^2}\right) - \rho\Phi$$

Gives the field equation

$$\nabla \cdot \left[ \mu\left(\frac{|\nabla\Phi|}{a_0}\right) \nabla\Phi \right] = 4\pi G\rho$$

# Relativistic MOND

- Phenomenological requirements
  - a) Return to GR (hence Newtonian gravity) when  $\nabla\Phi \gg a_0$
  - b) Reproduce MOND law when  $\nabla\Phi \ll a_0$
  - c) Reproduce cosmological observations like CMB and MPS
  - d) Reproduce the observed lensing effect
  - e) Propagate tensor mode GWs at the speed of light (GW170817)

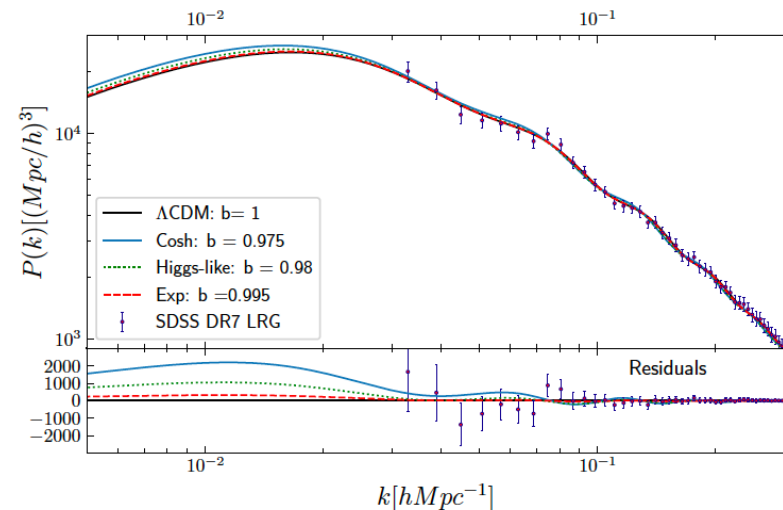
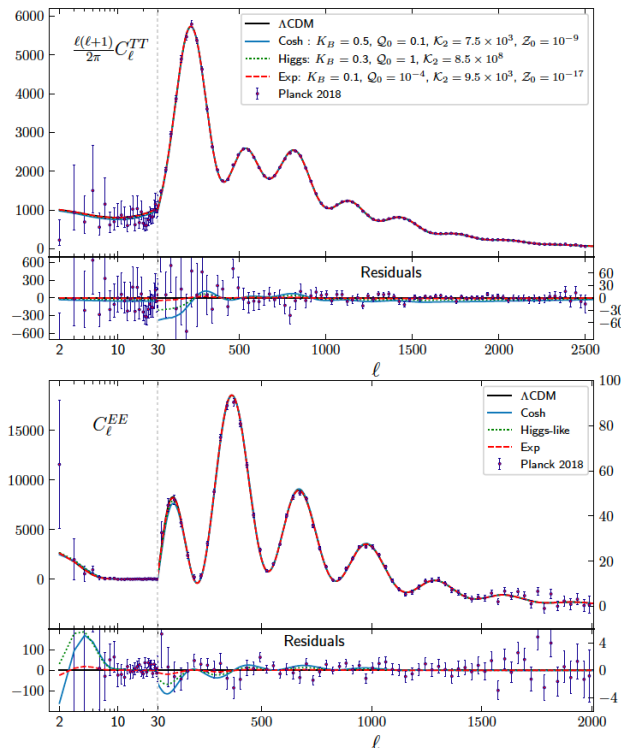
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# A new theory (2007.00082)

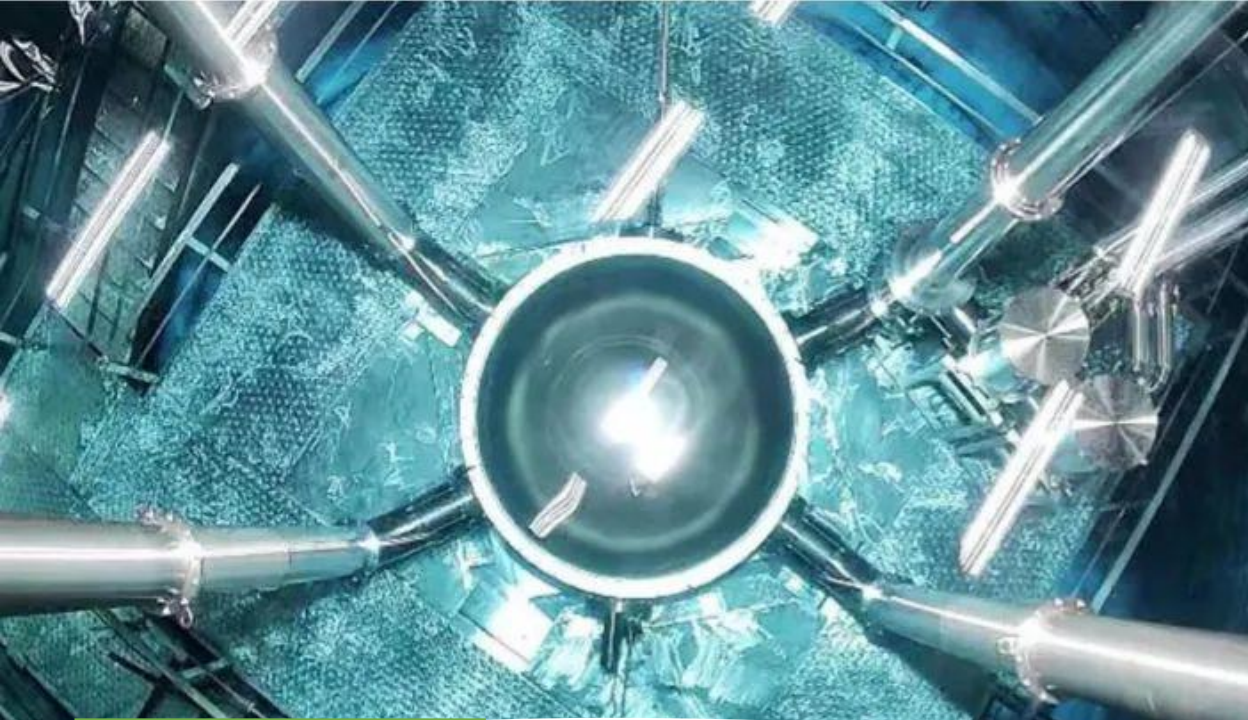
- An extra **scalar field  $\phi$**  and **vector field  $A^\mu$**  to compensate the gravity originally contributed by DM
- Different from DM paradigm



# Discussion

Dark matter paradigm	Relativistic MOND
1 parameter	5 parameters
Simple	Complicated
Almost fit with Observation	To be verified but can explain BTFR

Do we really need DM?



PandaX-4T

Yes and No!

- **Yes:** Simple enough to explain almost every observational facts
- **No:** We haven't detected any signal of DM particles

# Take home message

- A cosmological model without DM can now successfully reproduce the **key observables**: CMB and MPS
- Until now DM paradigm is sufficient for us. But if we still can not detect the DM particles in the next several decades, we might seek for the other solution.

# Questions

- Will this relativistic MOND help to solve **Hubble tension**?
- How can we **confirm the existence** of the extra fields?