



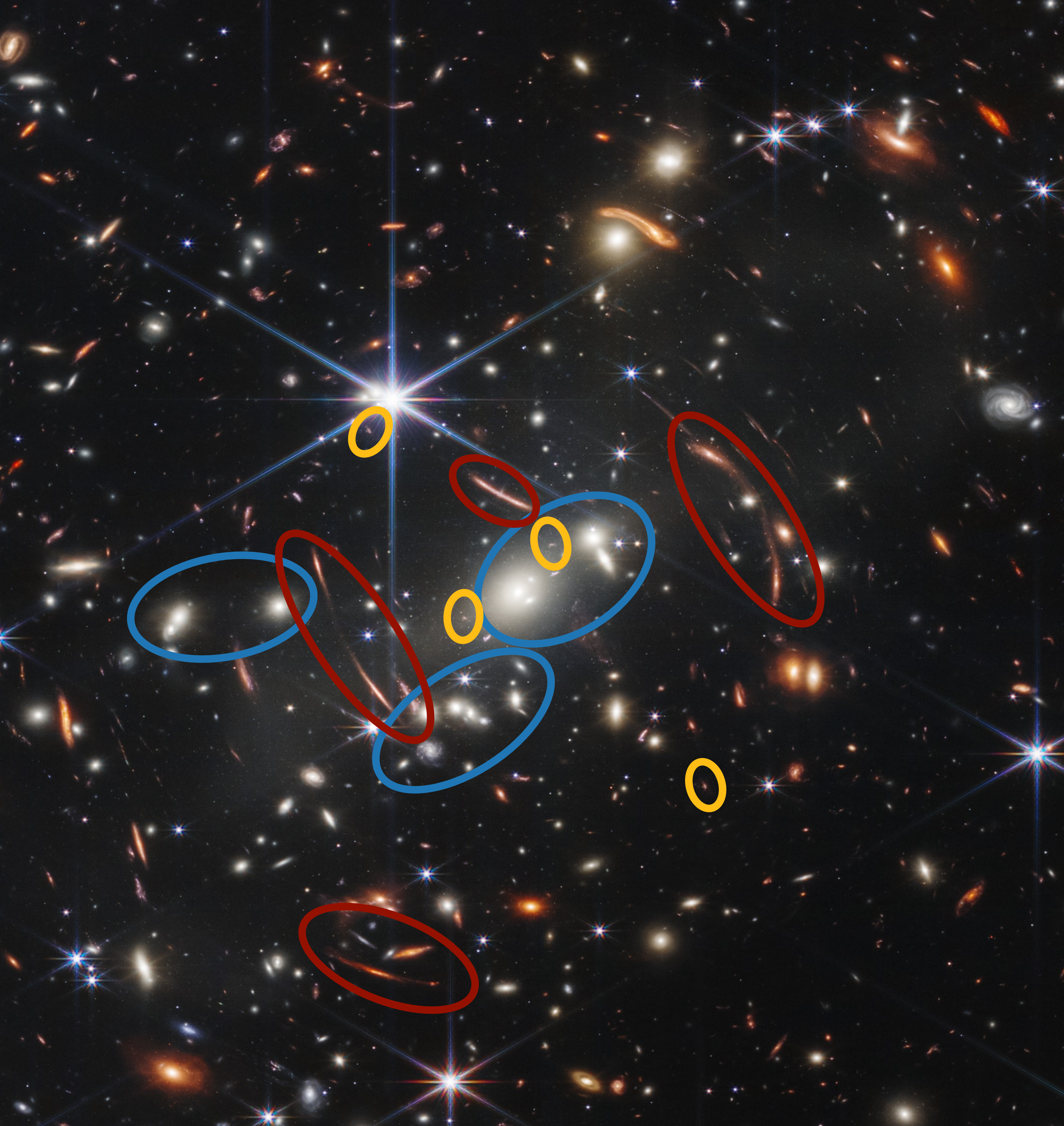
Cluster Lensing in the JWST Era

Applications of Cluster Lensing

Wenshuo Xu

Advisor: Dandan Xu

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SMACS J0723

Foreground
Galaxy Cluster

Arclet Image

Multiple-Image
System

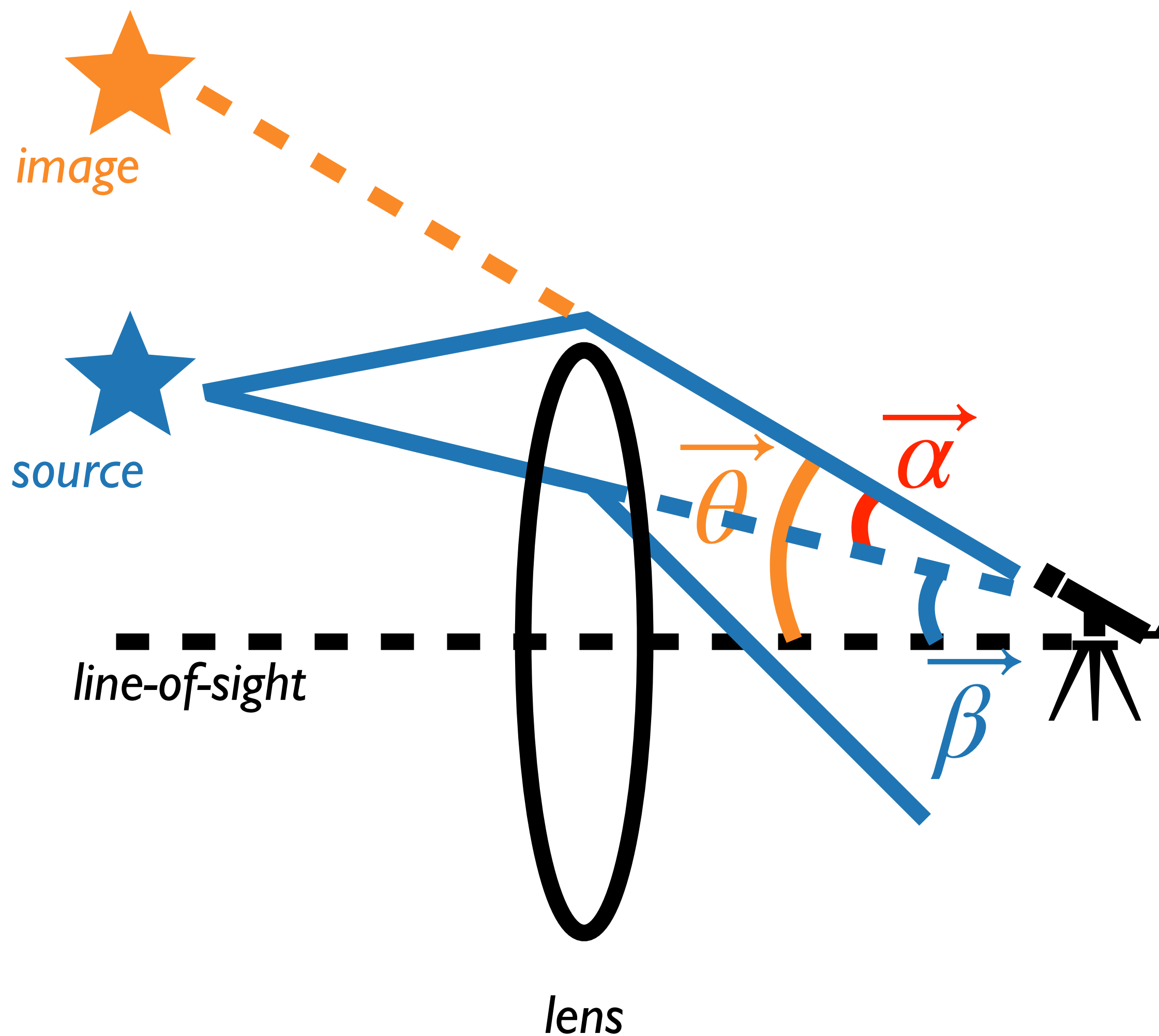
Outline

3 Steps to Be a “Strong Lensing Expert”

Study on Lens Properties

Study on Source Properties

Step 1 Deflection Effect



lens equation

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}$$

$\vec{\beta}$ (source plane): angular position of source

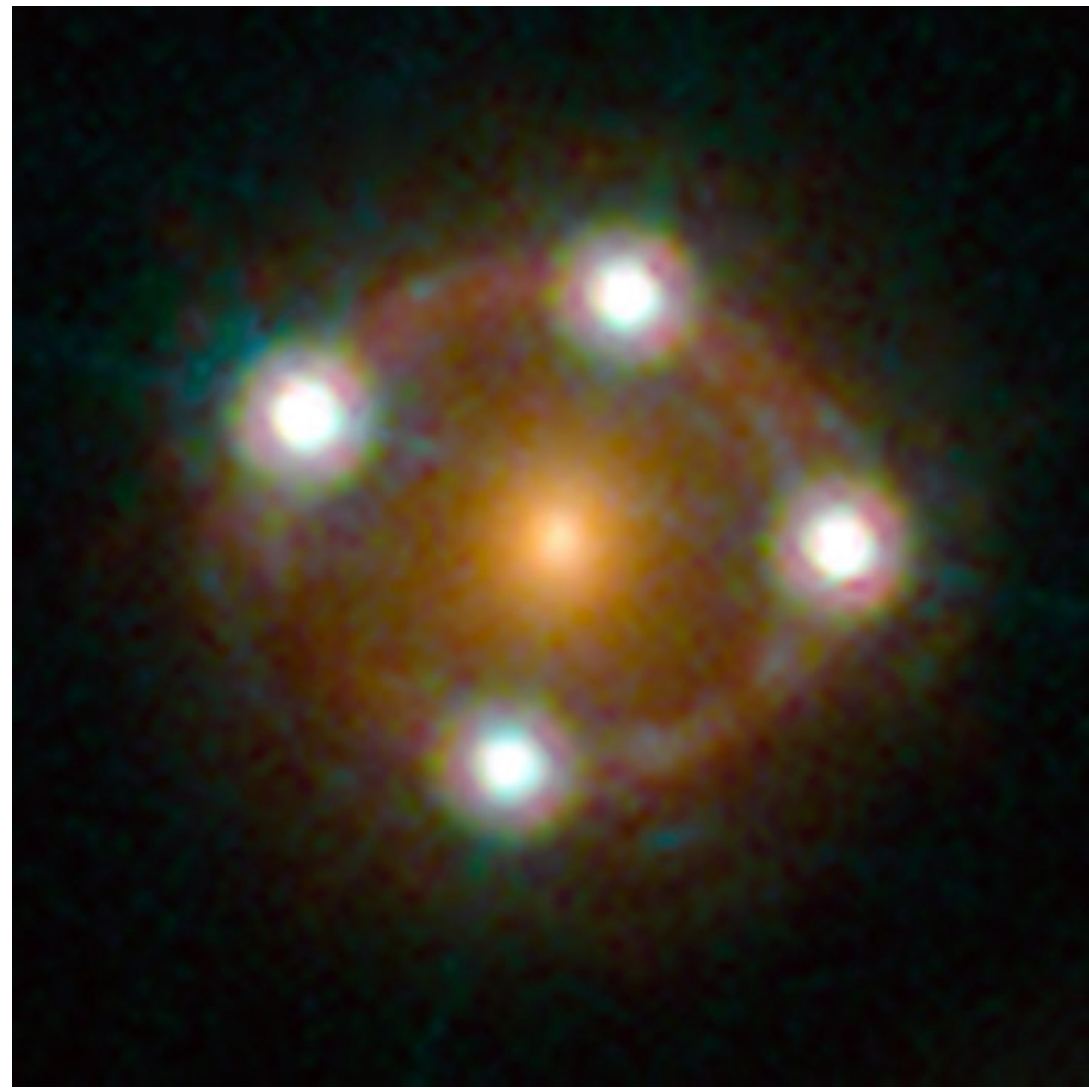
$\vec{\theta}$ (image plane): observed angular position of image

$\vec{\alpha}$: deflection angle

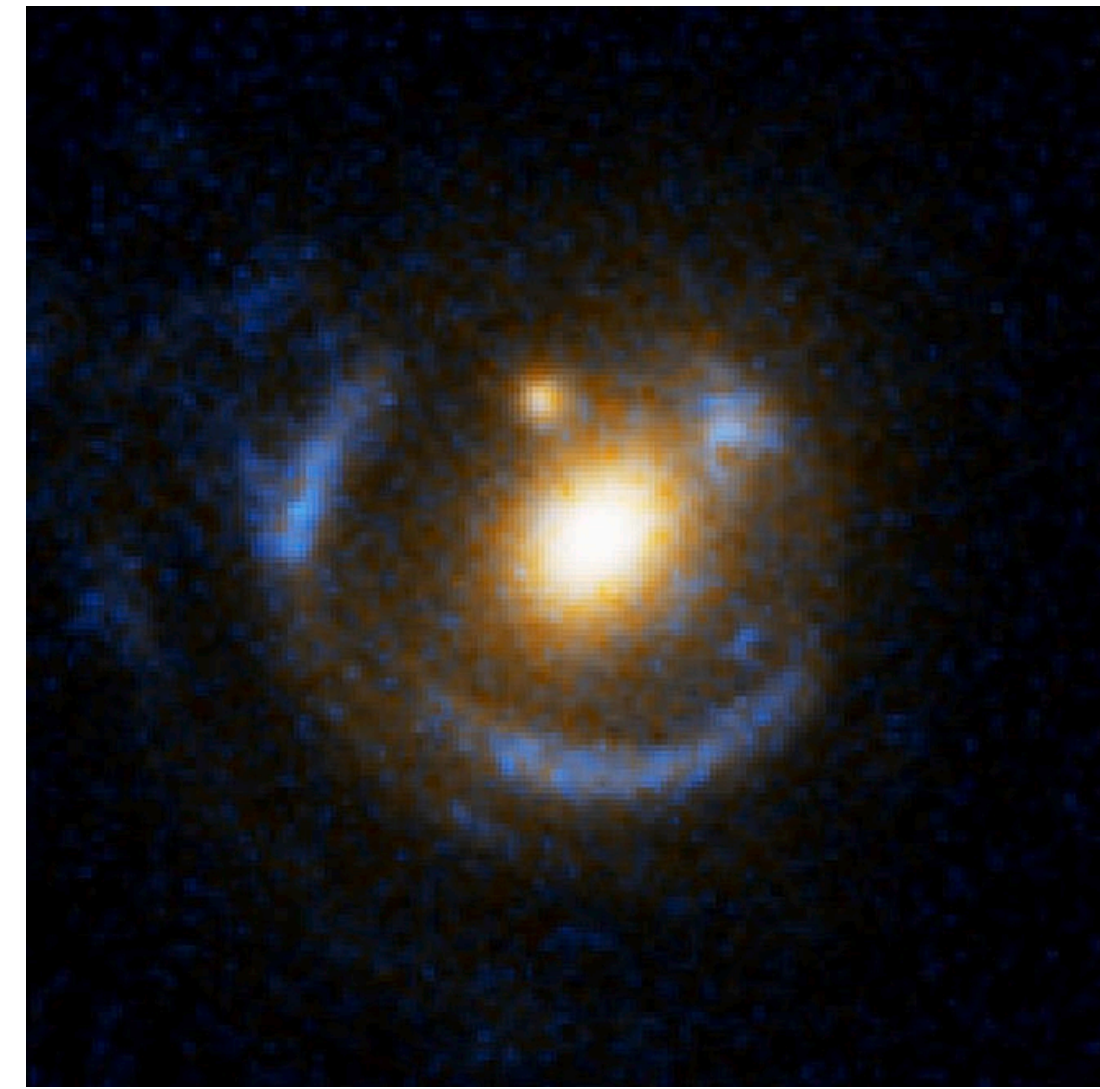
$$\vec{\alpha}(\vec{\theta}, \Sigma(\vec{\theta}), z_s, z_l)$$

↑
lens
surface density
distribution

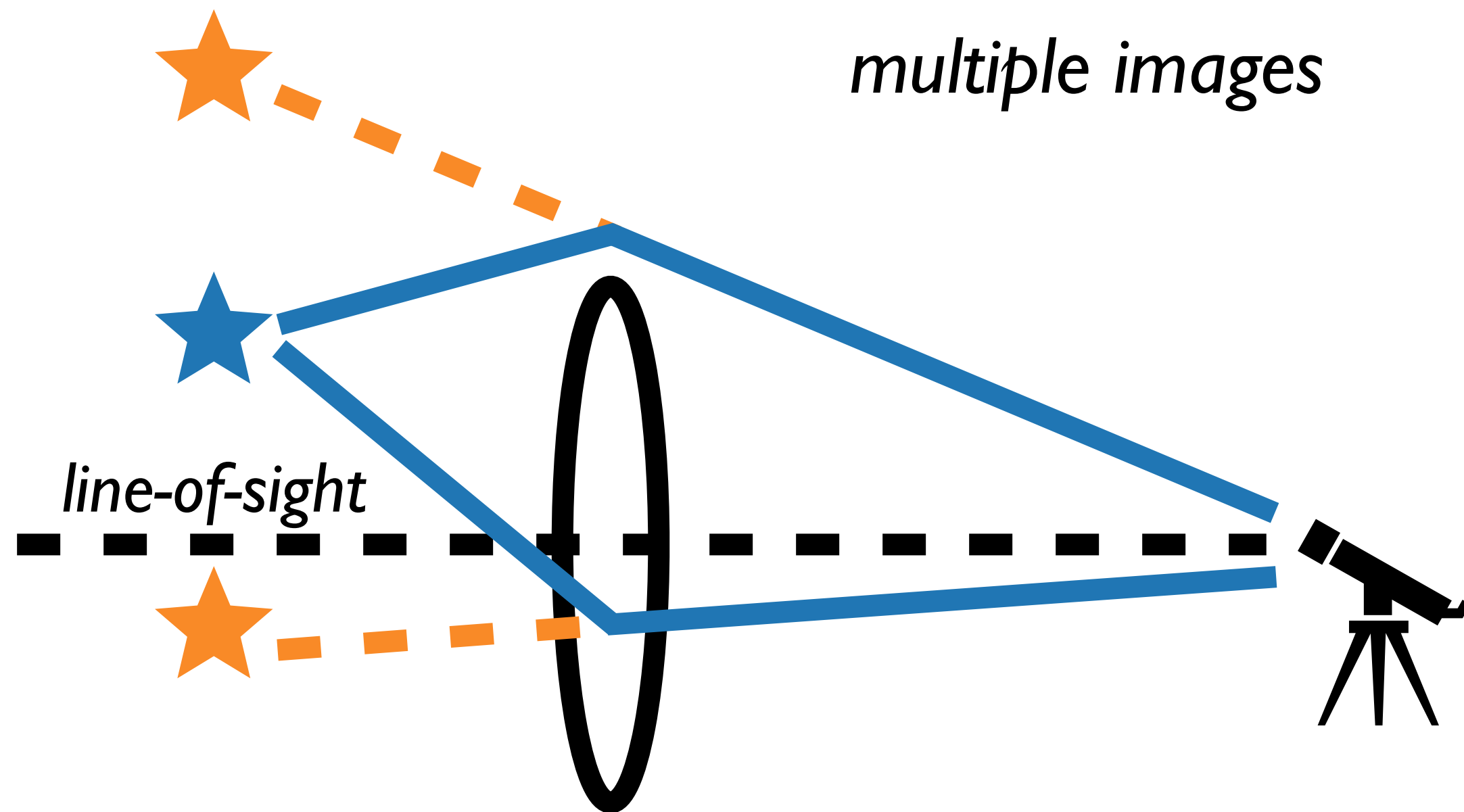
Step 1 Deflection Effect



multiple images



arc-like image



● extended sources in the universe

Step II Magnification Effect

$$\text{Flux (F)} = \text{Surface Brightness (S)} \times \text{Area (A)}$$

- Gravitational lensing conserves the surface brightness of source
- Gravitational lensing magnifies the area of source

$$\bar{\mu}_{\text{image}} = \frac{F_{\text{image}}}{F_{\text{source}}}$$

correct for source intrinsic flux

correct for source intrinsic size/area

magnification factor
(extended source)

Step II Magnification Effect

$$\text{Flux (F)} = \text{Surface Brightness (S)} \times \text{Area (A)}$$

- Gravitational lensing conserves the surface brightness of source
- Gravitational lensing magnifies the area of source

$$\bar{\mu}_{\text{image}} = \frac{F_{\text{image}}}{F_{\text{source}}}$$

“hard to know”

magnification factor
(extended source)

usually approximated with $\mu(\vec{\theta})$
in cluster lens correction

$$\mu(\vec{\theta}, \Sigma(\vec{\theta}), z_s, z_l)$$

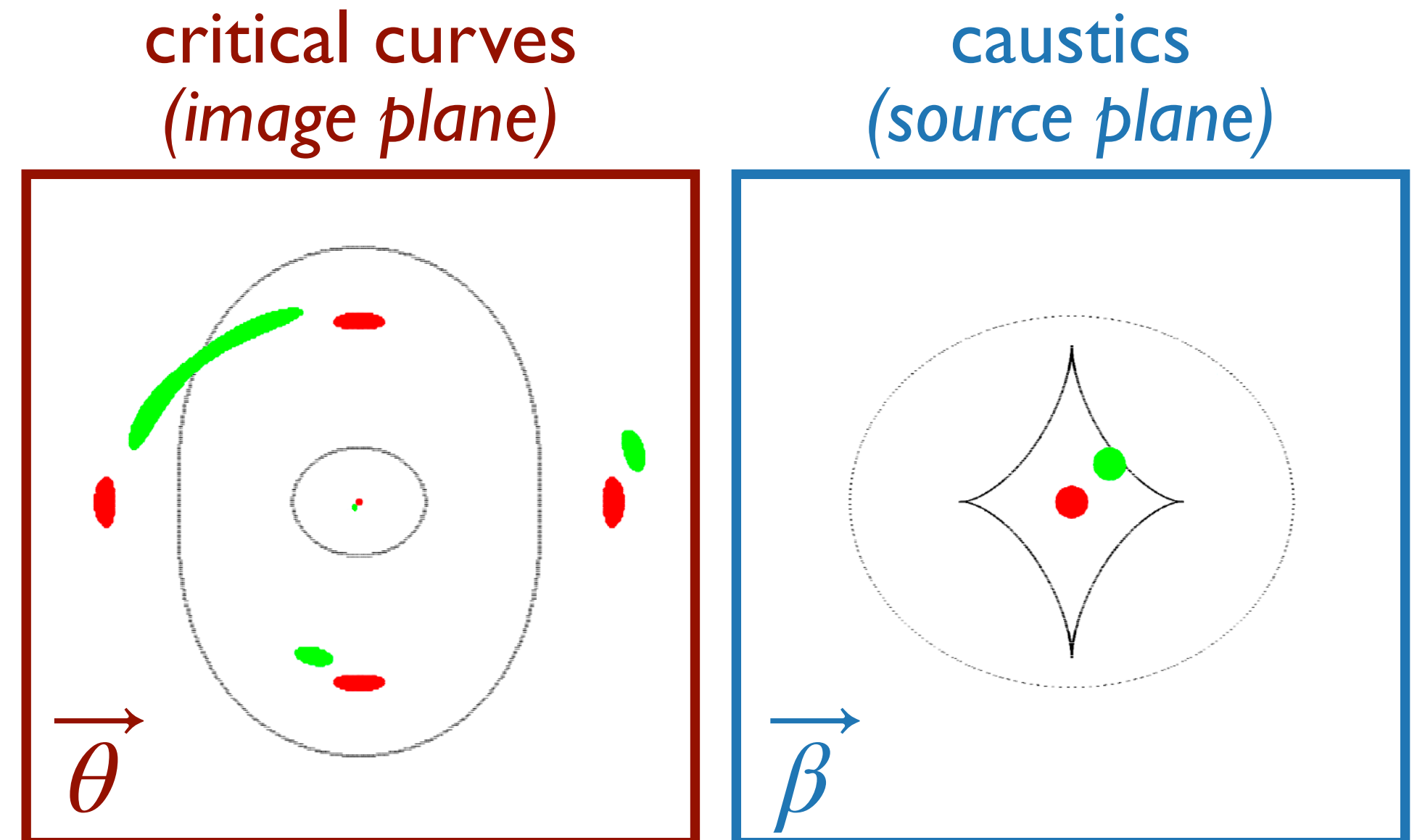
magnification factor
(infinitesimal source)

Step III Terminology

- critical curve and caustic

critical curve: positions on image plane
 $\{\vec{\theta}_c\}$ with infinite analytic
magnification factor $\mu(\vec{\theta}_c) = \infty$

caustic: positions on source plane
 $\{\vec{\beta}_c\}$ corresponding to critical curves



- The vicinity of critical curve has extreme magnification **gradient**
- Images merge around critical curves and form arclet
- Critical curve reveals the reach size of strong lensing effect
galaxy lens: ~ 1 arcsec
cluster lens: ~ 10 arcsec - 1 arcmin

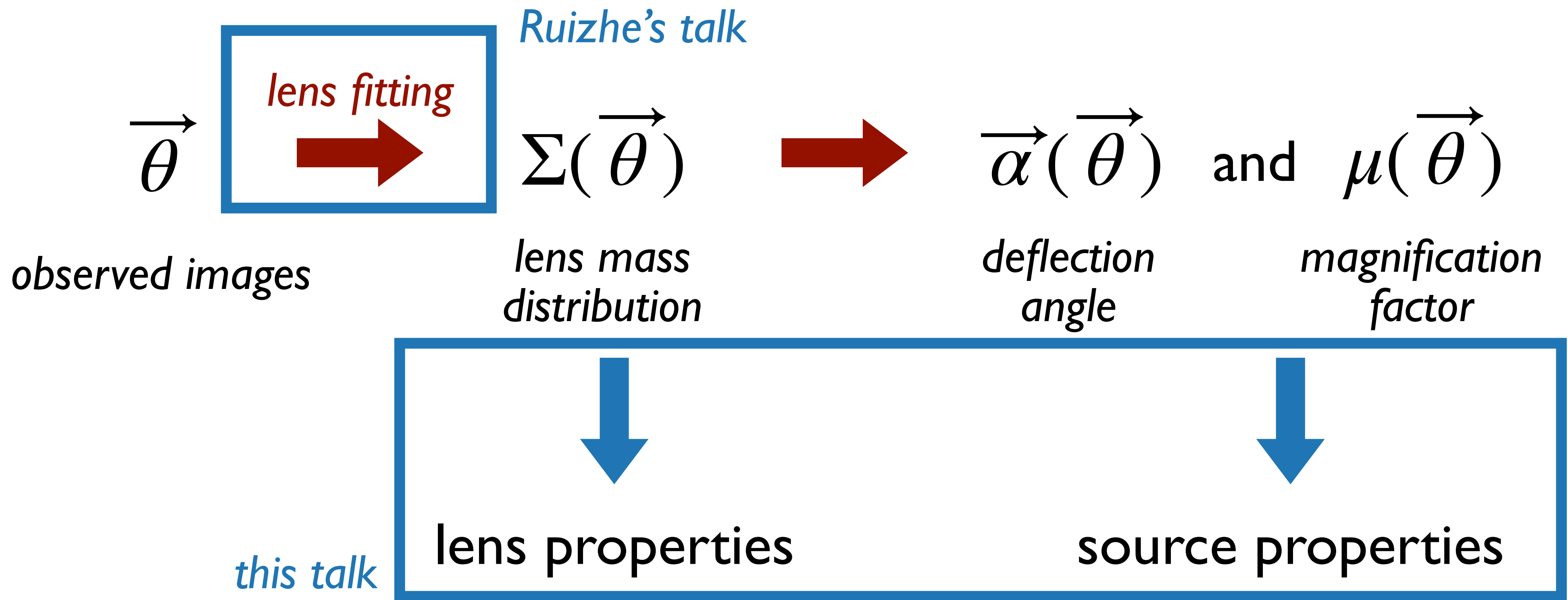
Strong Lensing Effect

- Deflection angle ($\vec{\alpha}$) and magnification factor (μ) depend on the mass distribution of lens and redshift.
- Gravitational lensing conserves the surface brightness of source and magnifies the area.
- Critical curve represents the positions with extreme magnification factor on image plane.
Images merge around critical curve and form arclet.

Methodology

lens equation: $\vec{\beta} = \vec{\theta} - \vec{\alpha}$ $\vec{\alpha}(\vec{\theta}, \Sigma(\vec{\theta}), z_s, z_l)$

Only image plane $\vec{\theta}$ is observable.



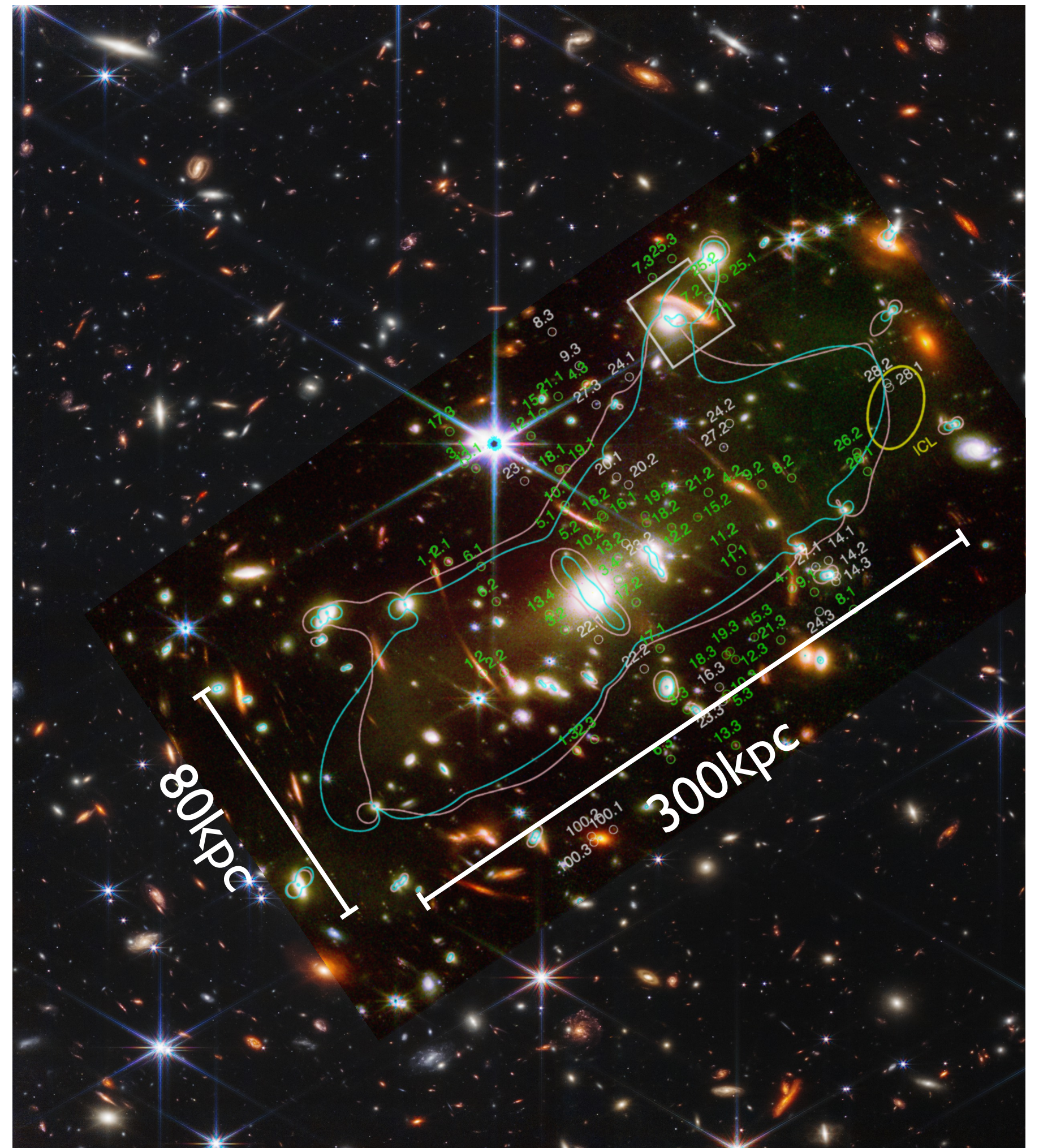
Study on Lens

- Gravitational lensing traces the distribution of **total mass**.

➔ *luminous matter, **dark matter***

- Strong lensing only constrains the mass distribution at the core of cluster.

➔ *combine with other methods (e.g. weak lensing, X-ray) to study large-scale mass distribution*



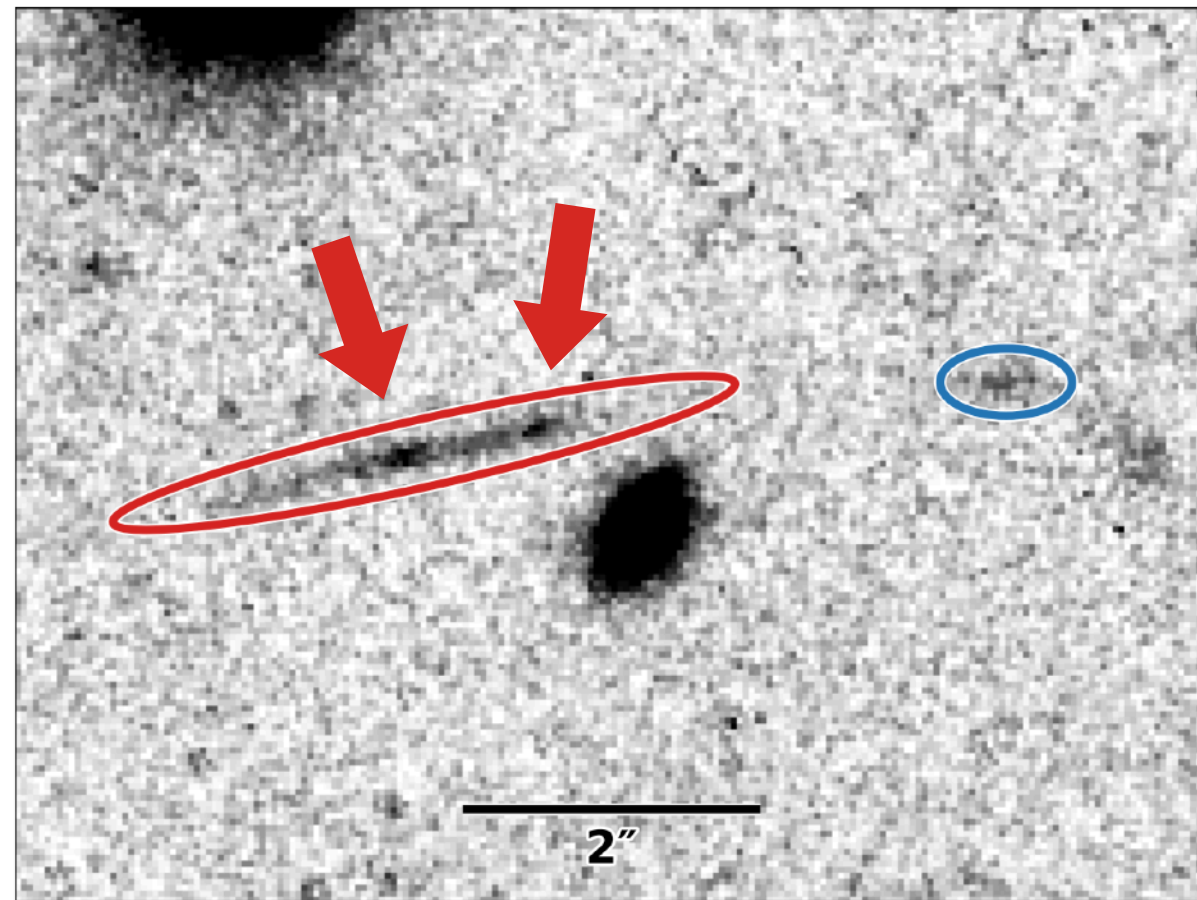
(Mahler et al. 2022)

Study on Background Sources

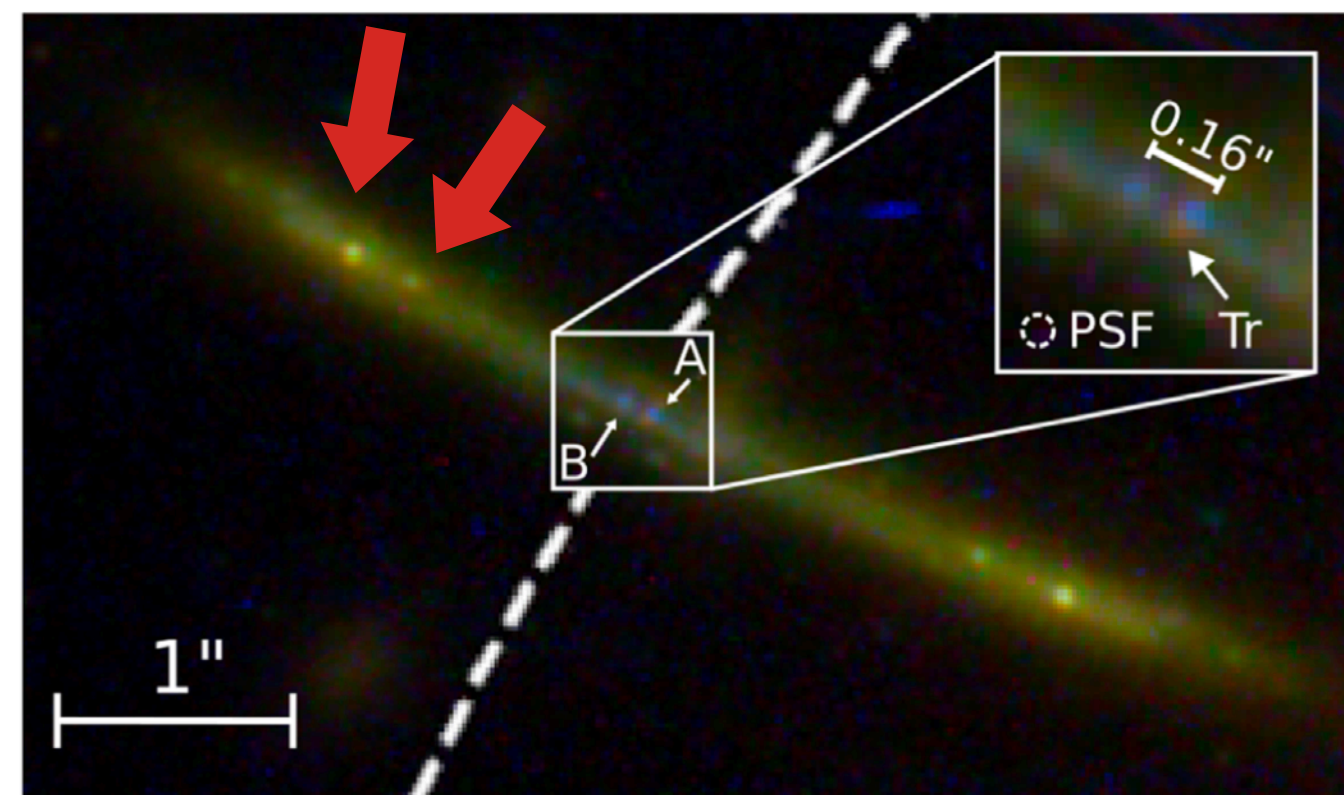
- Zoom in to study substructures of high- z objects
- Facilitate identifying extremely high- z objects

Study on Background Sources

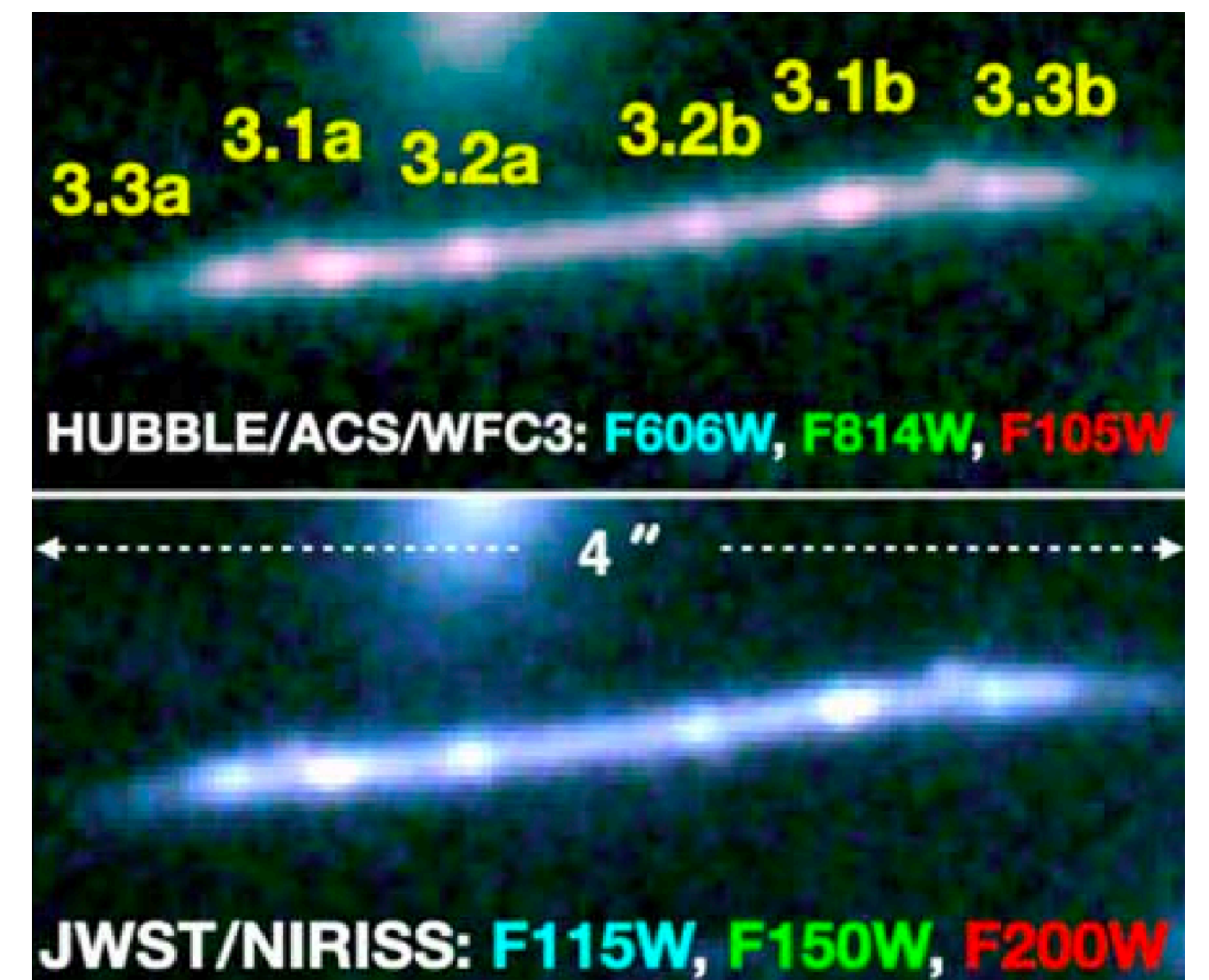
- Zoom in to study substructures of high-z objects



WHL0137-08 cluster field
photometric $z_p \sim 9$
(Bradley et al. 2022)



SMACS 0723 cluster field
spectroscopic $z_s = 1.43$
(Pascale et al. 2022)



Abell 2744 cluster field
spectroscopic $z_s = 4.0$
(Vanzella et al. 2022)

- Facilitate identifying extremely high-z objects

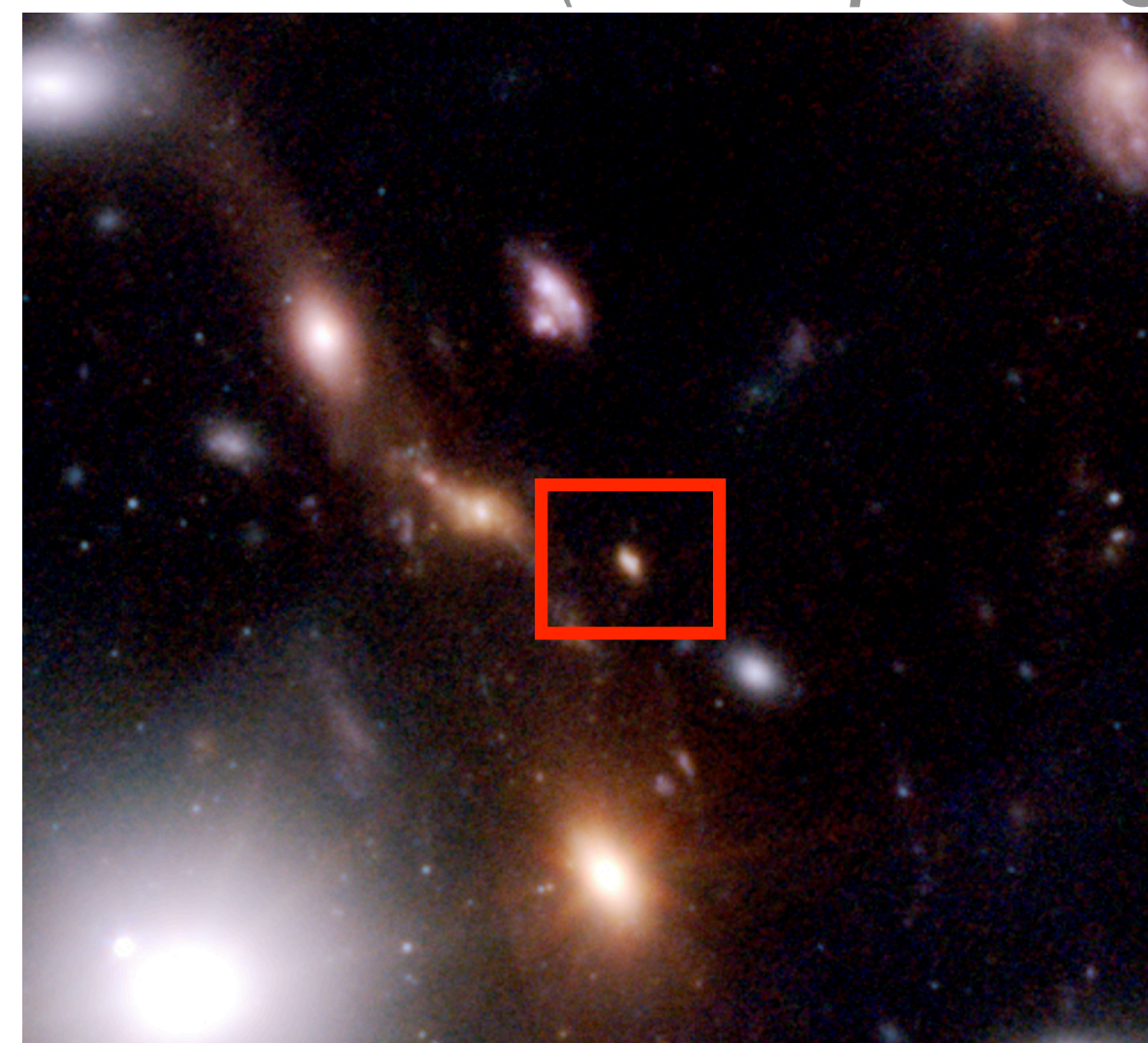
Study on Background Sources

- Zoom in to study substructures of high-z objects

(same plotting scale)



*arclet formed by
two merging images*



third image

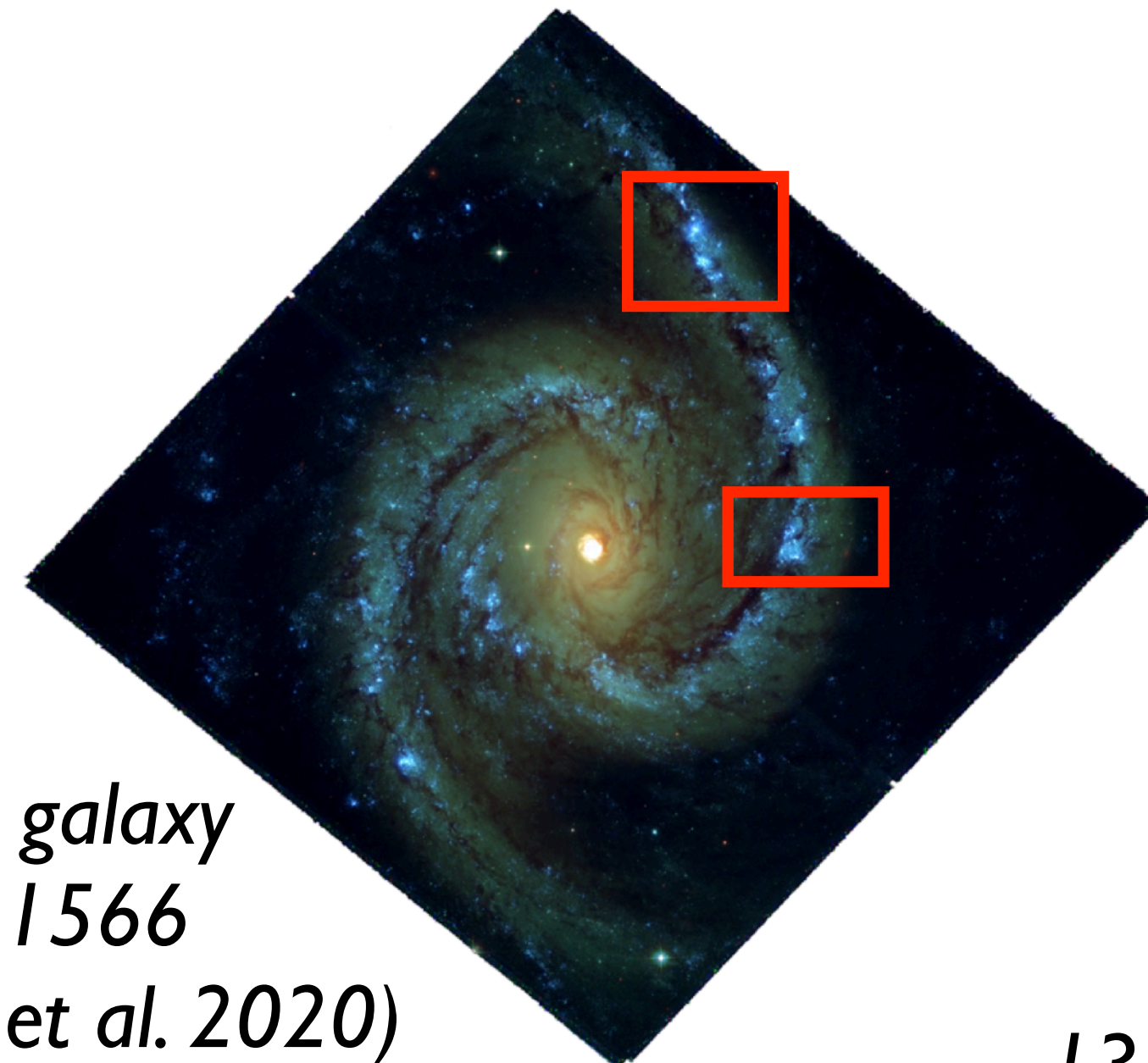
- Facilitate identifying extremely high-z objects

Source Properties: Clumpy Star-Forming Regions

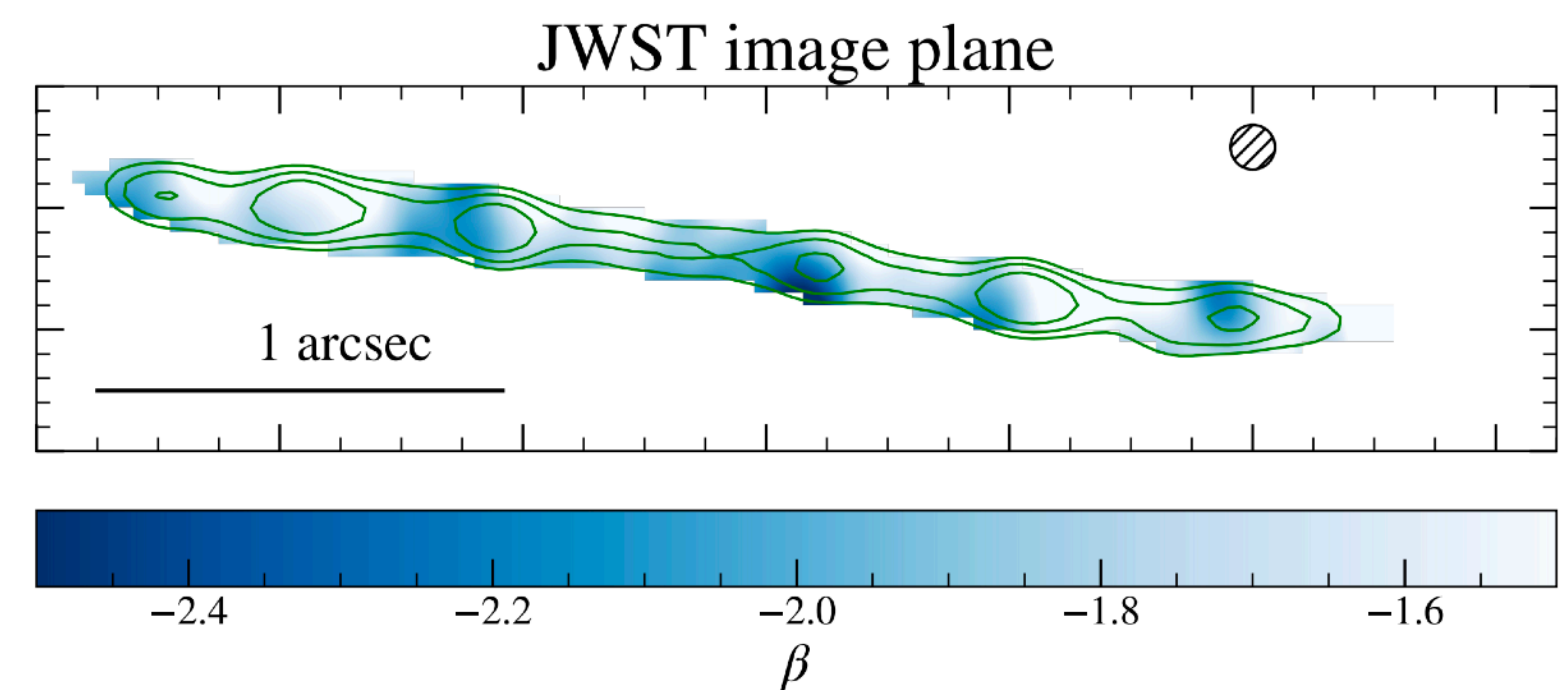
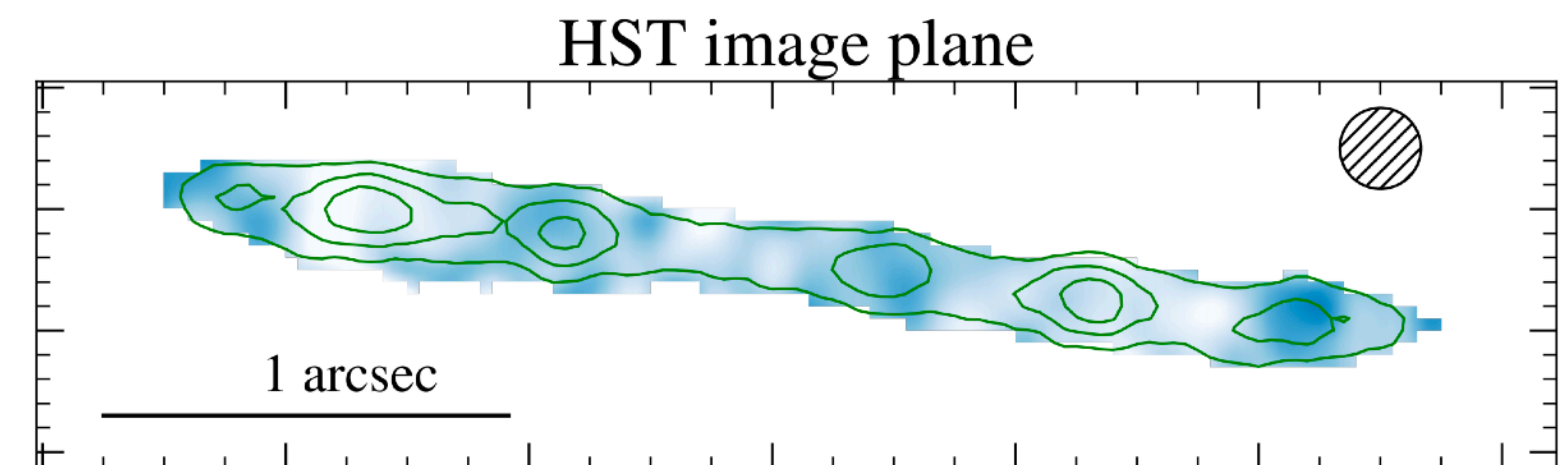
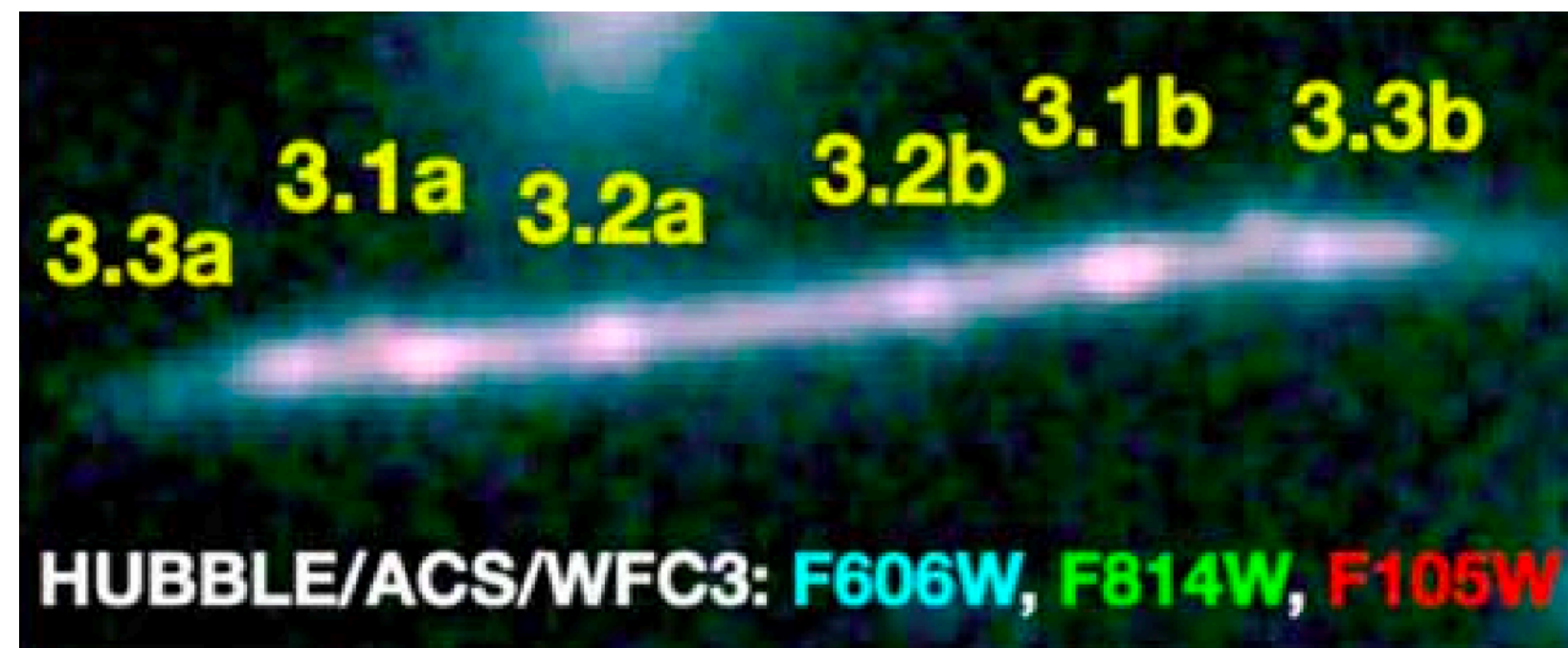
- JWST **near-infrared** observation waveband: $0.6 \mu\text{m} - 5 \mu\text{m}$
(imaging&spectroscopic)
➔ correspond to rest-frame **UV & visible** band for high- z galaxies
- Observations in local universe indicates a hierarchical organization of star formation.
➔ *sub-kpc clumps, pc-scale stellar clusters*

need extremely high resolution,
cluster lensing **HELPS!**

nearby galaxy
NGC 1566
(Gouliermis et al. 2020)

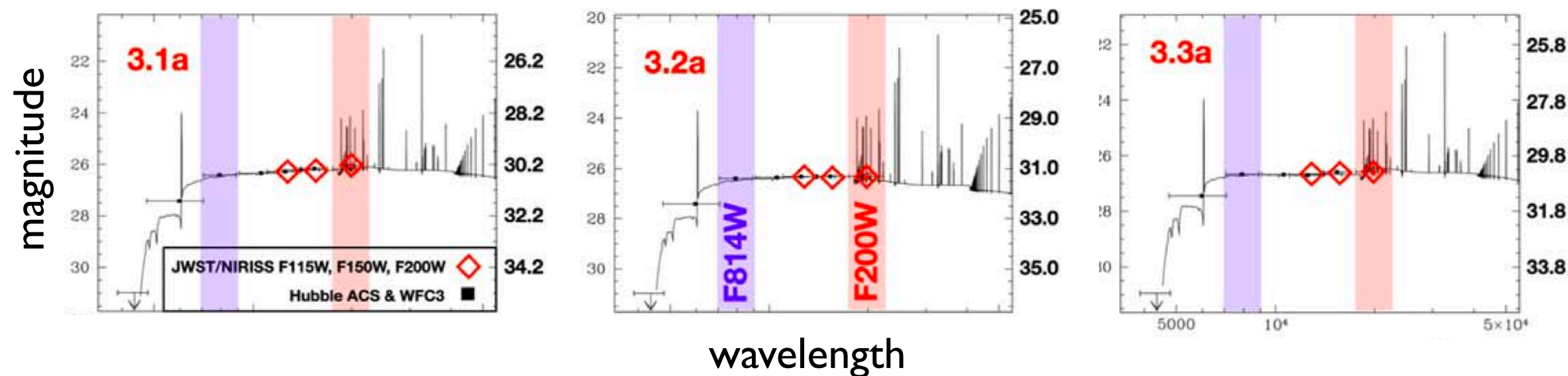


Source Properties: Clumpy Star-Forming Regions



*UV slope(β) map of the lensed arclet
(Lin et al. 2022)*

*SED fitting of the 3 knots
(Vanzella et al. 2022)*

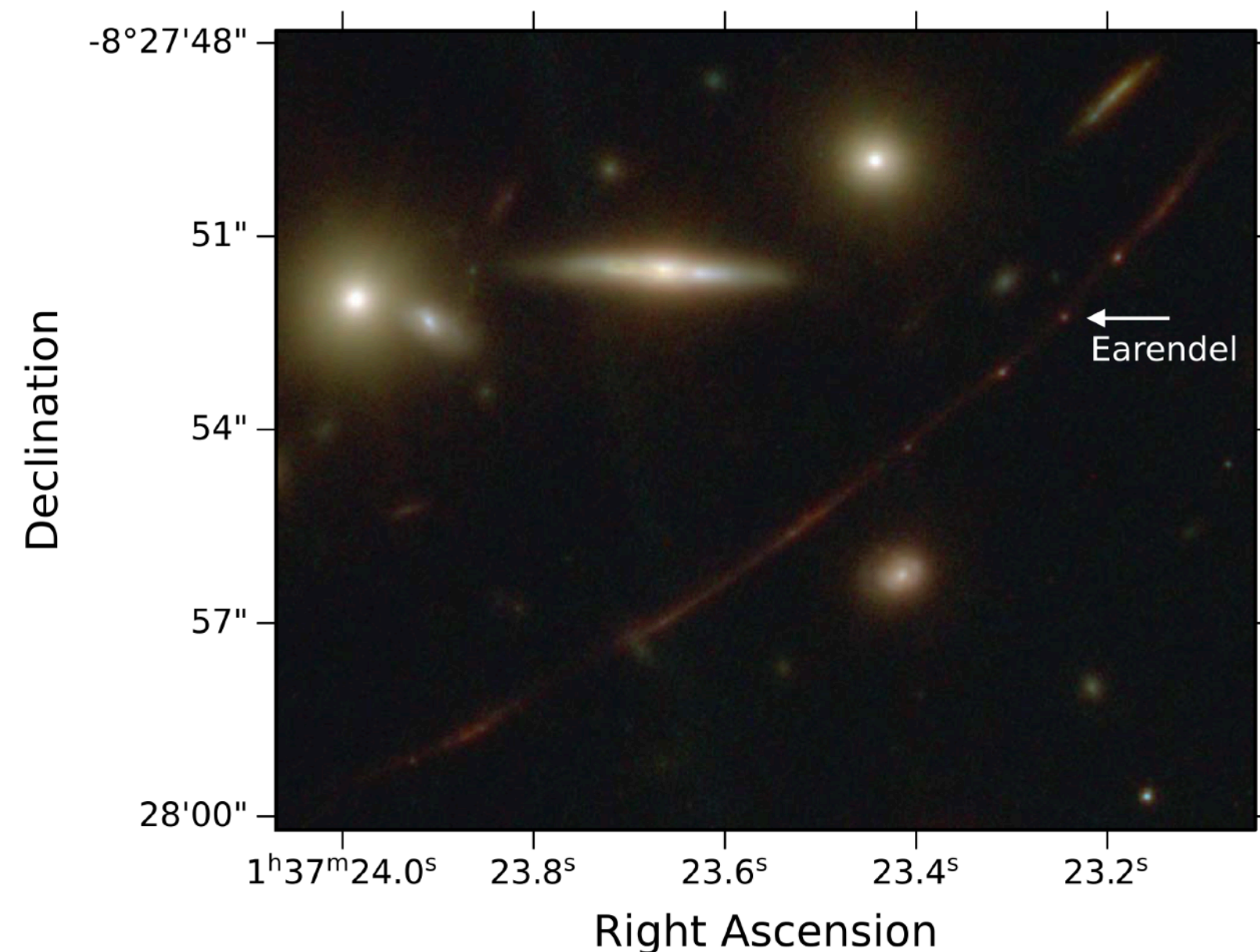


- physical properties of the substructure

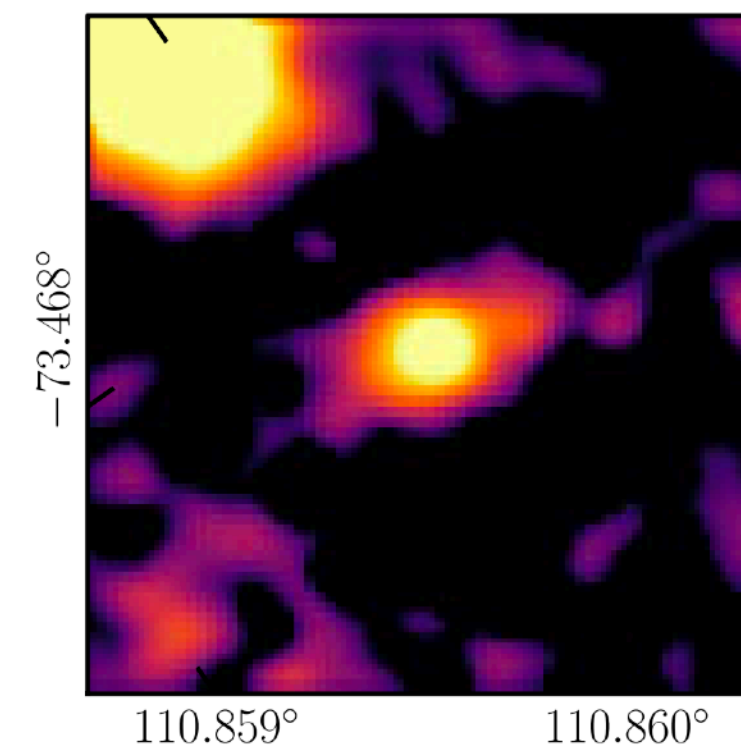
- spatial distribution of properties

Study on Background Sources

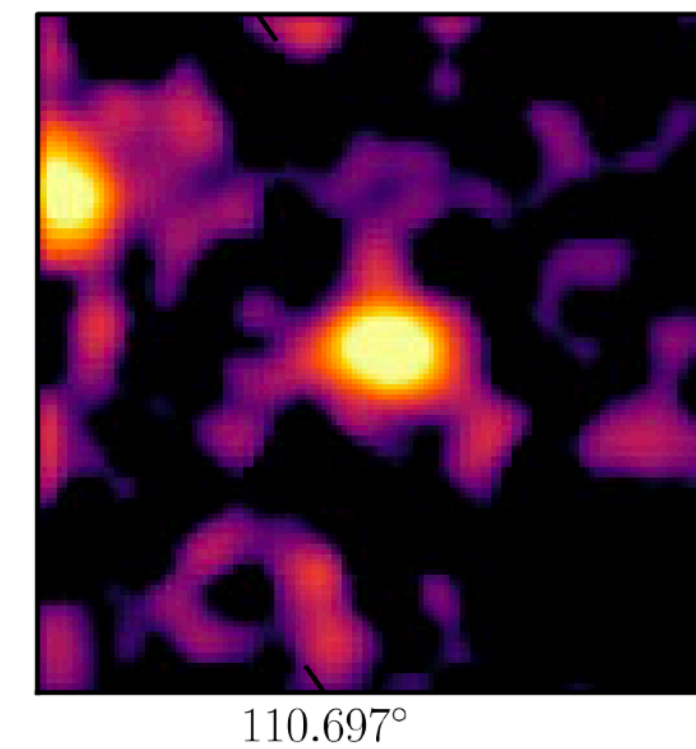
- Zoom in to study substructures of high-z objects
- Facilitate identifying extremely high-z objects



*most distant star Earendel
(Welch et al. 2022)*



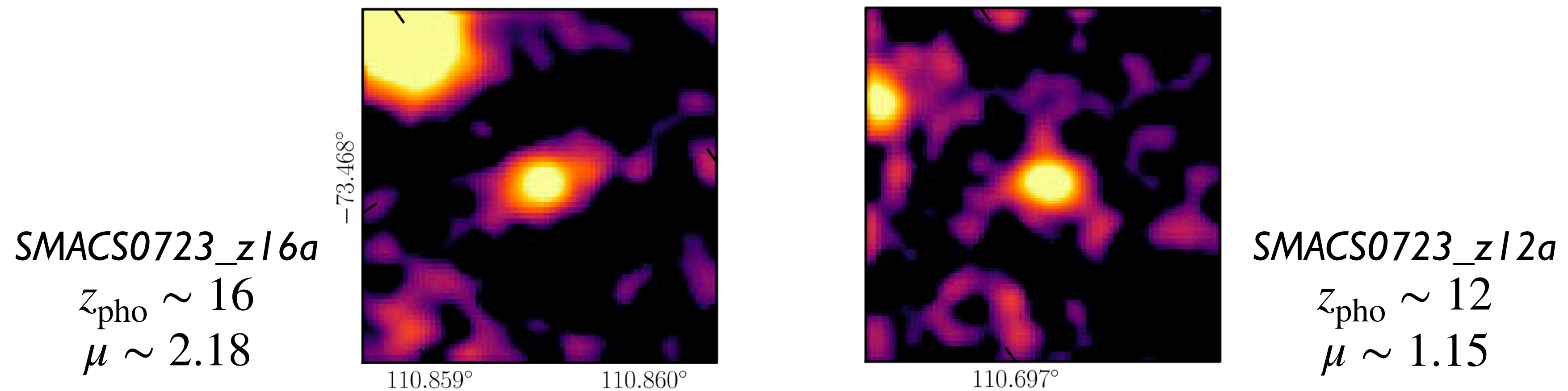
SMACS0723_z16a
 $z_{\text{pho}} \sim 16$
 $\mu \sim 2.18$



SMACS0723_z12a
 $z_{\text{pho}} \sim 12$
 $\mu \sim 1.15$

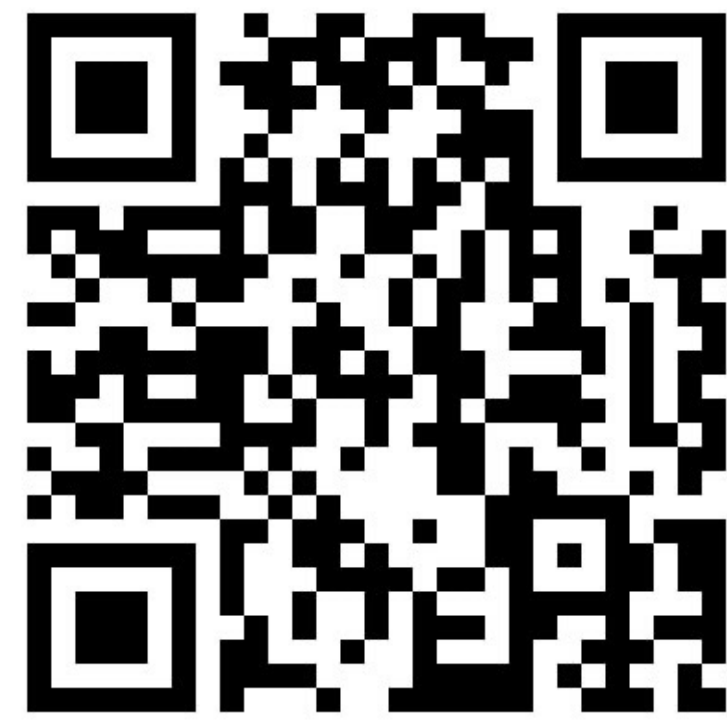
*extremely distant galaxy candidates
(Atek et al. 2022)*

Source Properties: Biases from Lensing Effect



- Gravitational lensing magnifies the total flux of high-z galaxies and modifies intrinsic properties.
- ➔ *intrinsic luminosity, stellar mass, scaling relations at high redshift*
- Correction of lensing magnification effect depends on $\Sigma(\vec{\theta})$.
- ➔ *bias and scatter in different lens models*

Summary



- Cluster lensing plays an essential role in the JWST era. It helps to study the properties of foreground cluster and background source.
- Magnification effect of cluster lensing greatly facilitate identifying and studying high redshift galaxies.
- Correction for magnification effect is a must, and it depends on the fitting of lens mass distribution. The improved capability of JWST can help to model the mass distribution of lens much more precisely.

Magnification Factor

- more natural to define magnification factor for extended sources as **area ratio**

$$\mu = \frac{\delta^2 \vec{\theta}}{\delta \vec{\beta}^2} \text{ (variation)}$$

- use differentiation to approximate for infinitesimal source

$$\mu = \frac{\vec{\theta} \, d\vec{\theta}}{\vec{\beta} \, d\vec{\beta}} \text{ (differentiation)} + \vec{\beta} = \vec{\theta} - \vec{\alpha} \rightarrow \mu(\vec{\theta}, \Sigma(\vec{\theta}), z_s, z_l)$$

$\vec{\alpha}(\vec{\theta}, \Sigma(\vec{\theta}), z_s, z_l)$