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THCA Student Seminar

# A GLIMPSE INTO GRAVITATIONAL WAVE SCIENCE

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Oct. 13, 2017

# Outline

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- Physical Nature of GWs
- Astronomical sources of GWs
- Detection techniques
- Recent LIGO results

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# Part I. Physical Nature of GWs

# What is GW?

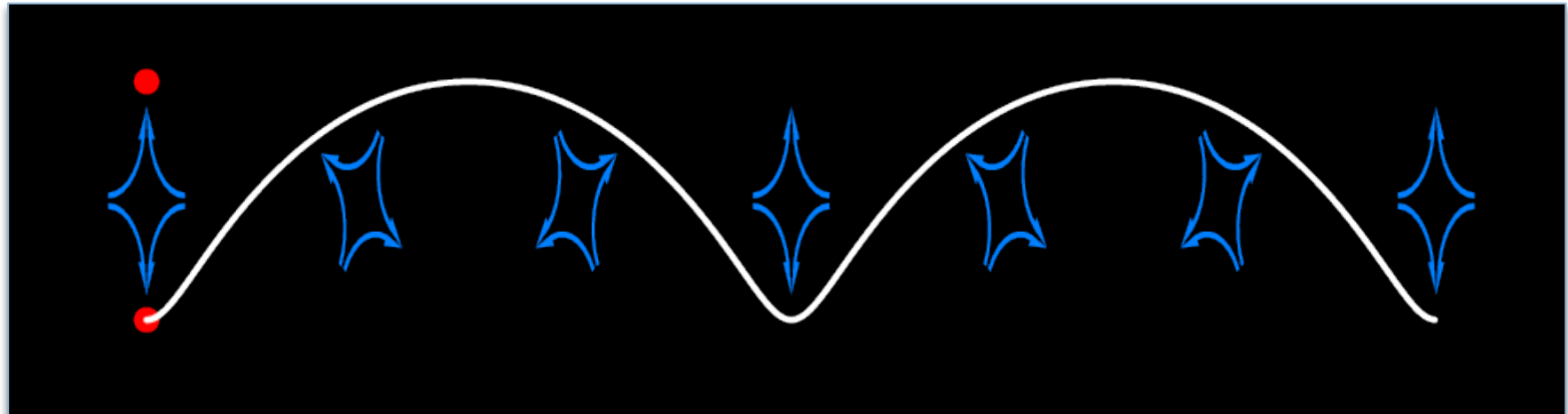
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## □ General relativity predicts:

Time-changing gravitational tidal field

➡ propagates out **at speed  $c$**

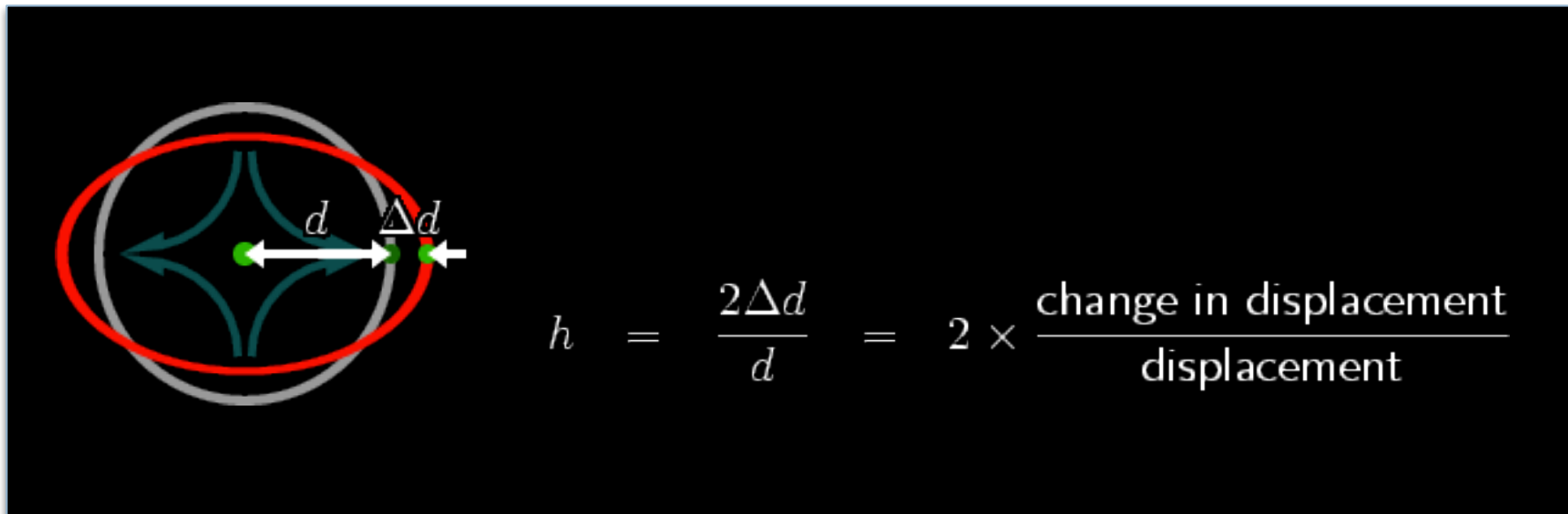
➡ **gravitational radiation!**



# Effect of GW on test masses

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- GW “**pushes and pulls**” on nearby test masses
  - The **proper distance** between them is changed
  - The fractional change is denoted by  $h$ , the “**strain**” field.
  - $h$  is related to the **metric perturbation** in a full GR



# Spin-2 nature of GW

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- A GW can have two distinct polarization states:



$h_+$  polarization



$h_x$  polarization

- Divergence-free, pure strain
- These states do not change under a 180 degree rotation → graviton is **massless** with **spin 2**

# Quadrupole nature of GW radiation

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E&M

Static coulomb field:  $E \sim \frac{Q}{r^2} \Rightarrow \cancel{\frac{\dot{Q}}{r}}$

Static dipole field:  $E \sim \frac{\mathbf{d}}{r^3} \Rightarrow \frac{\dot{\mathbf{d}}}{r^2} \Rightarrow \frac{\ddot{\mathbf{d}}}{r}$  **Dipole radiation!**

GW

Static monopole field:  $g \sim \frac{M}{r^2} \Rightarrow \cancel{\frac{\dot{M}}{r}}$

Static dipole field:  $g \sim \frac{\mathbf{d}}{r^3} \Rightarrow \frac{\dot{\mathbf{d}}}{r^2} \Rightarrow \cancel{\frac{\ddot{\mathbf{d}}}{r}}$  momentum conservation

Static quadrupole field:  $g \sim \frac{\mathcal{I}}{r^4} \Rightarrow \Rightarrow \frac{\ddot{\mathcal{I}}}{r}$  **Quadrupole radiation!**

# Why is GW so weak?

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$$\text{E\&M} \quad \frac{P}{E} \approx \frac{\langle \ddot{\mathbf{d}} \ddot{\mathbf{d}} \rangle}{E} \sim \frac{f^4 Q^2 s^2}{Q^2/s} \sim f^4 s^3 \sim (\lambda f)^3 \left( \frac{s}{\lambda} \right)^3 f \sim v^3 f$$

$v \ll 1$

Size of source

GHz  
~ THz

$$\text{GW} \quad \frac{P}{E} \approx \frac{\langle \ddot{\mathbf{I}} \ddot{\mathbf{I}} \rangle}{E} \sim \frac{f^6 M^2 s^4}{M^2/s} \sim f^6 s^5 \sim (\lambda f)^5 \left( \frac{s}{\lambda} \right)^5 f \sim v^5 f$$

$v \ll 1$

Hz ~ kHz

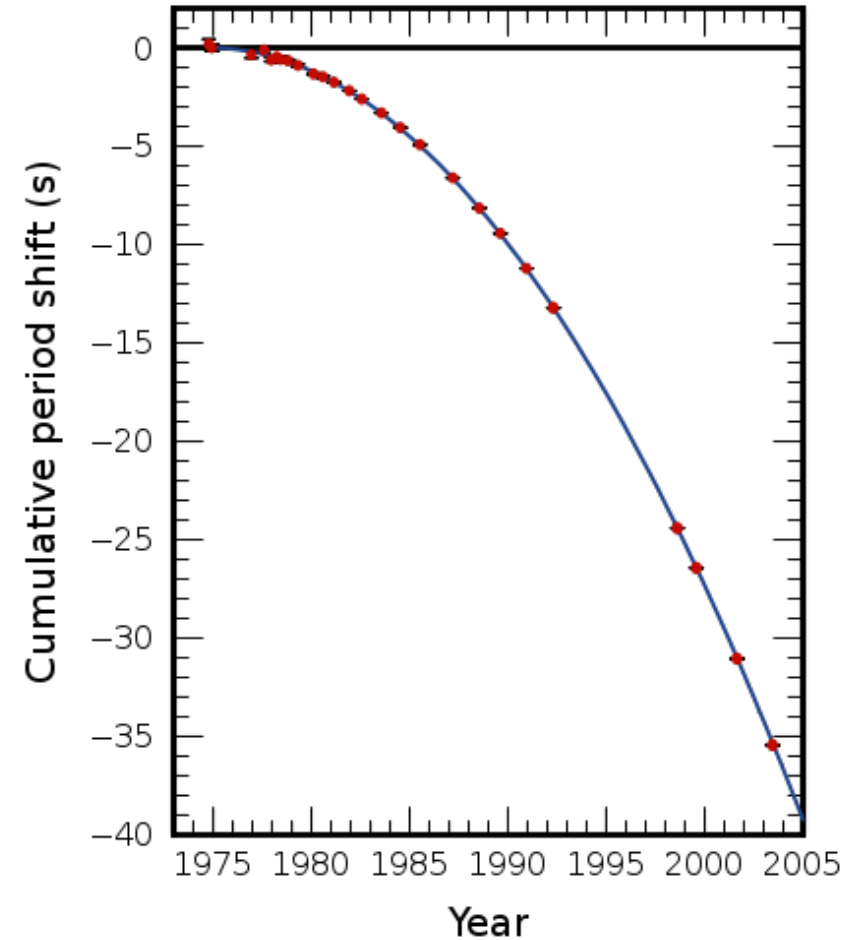
- **GW also interacts *very weakly* with matter**
  - **Dust or ideal fluid:** no response to the pure strain field of GW.
  - **Viscous or elastic matter:** attenuation/dispersion negligible.
  - Array of good emitters (NSs): “GW blackbody”?



# History note: NS-NS orbital decay

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- PSR 1913+16  
(Hulse & Taylor, 1975,  
Nobel prize 1993)
  - Pulsar + NS binary
  - 1.4+1.4 solar masses
  - Orbital period 7.75hr
  - Separation ~several solar radii
  - First indirect evidence for GW
  - ~A dozen detected now by radio



# Calculating the strain of a GW

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$$g \approx \frac{\ddot{\mathcal{I}}}{r} \rightarrow h \approx \frac{\ddot{\mathcal{I}}}{r}$$
$$h \approx \frac{Ms^2 f^2}{r} = \frac{r_{\text{sch}} s^2}{r(cT)^2}$$



**At the end of its life**

$$r_{\text{sch}} \sim 3\text{km}, s \sim 30\text{km}, T \sim 10^{-3} \text{ s}$$

For a system in our own galaxy ( $r \sim 10\text{kpc}$ ):  $h \sim 10^{-18}$

For a system in Virgo cluster ( $r \sim 10\text{Mpc}$ ):  $h \sim 10^{-21}$

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## Part II. Astronomical sources of GWs

# Binary GW sources

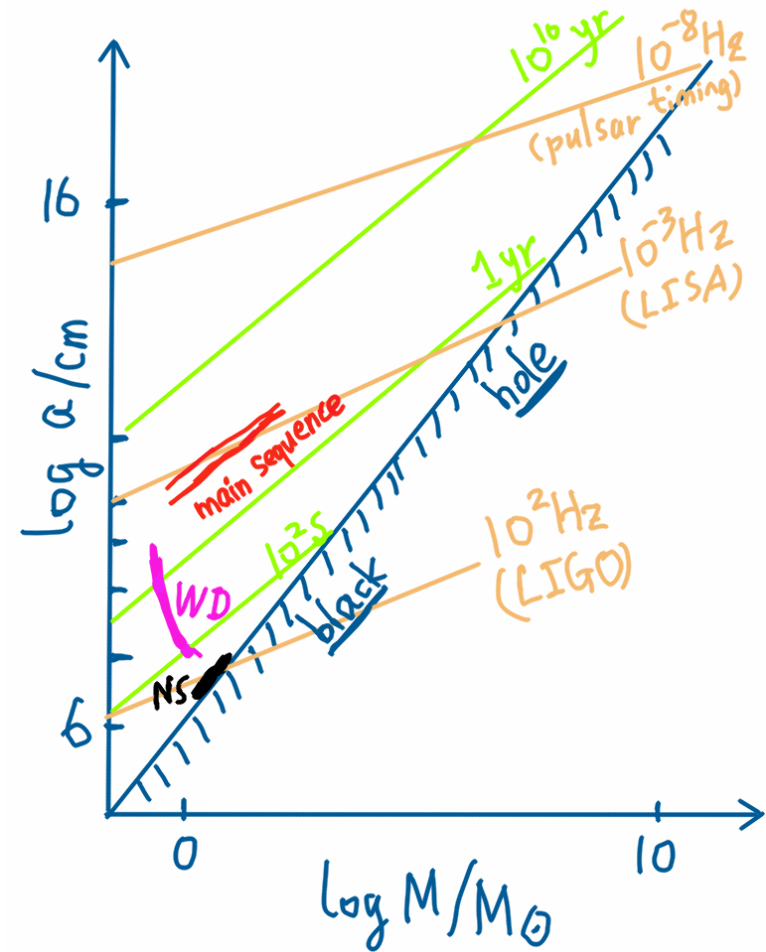
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$$f_{\text{GW}} = 2/P_{\text{orb}}$$

$$t_{\text{merger}} \propto M^{-5/3} f_{\text{GW}}^{-8/3}$$

For a  $1M_{\odot} + 1M_{\odot}$  binary

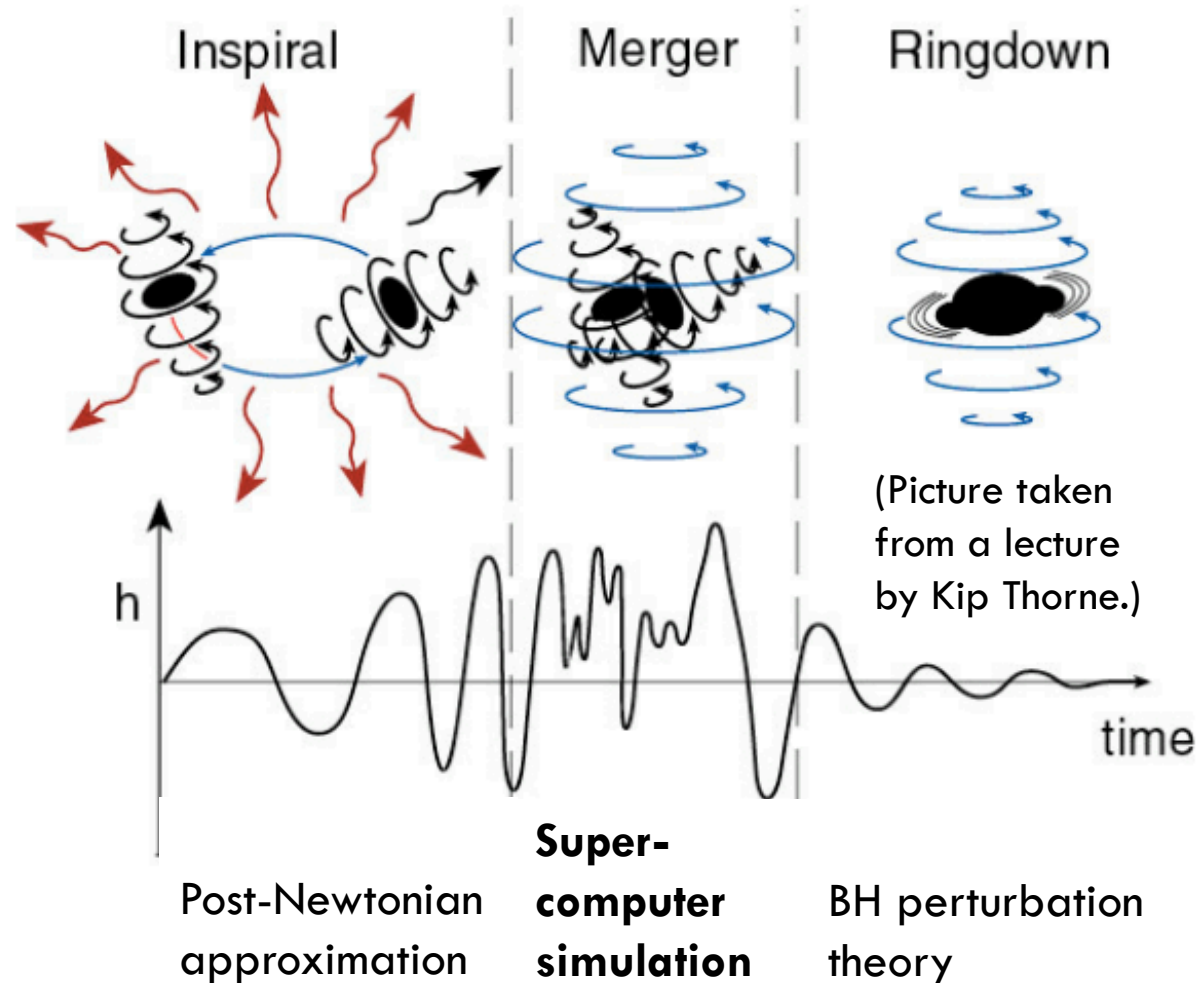
GW frequency	Merger time
$4.5 * 10^{-5}$ Hz	$10^{10}$ yr
$4.5 * 10^{-2}$ Hz (LISA band)	$10^2$ yr
45 Hz (LIGO band)	300s



(Adapted from an online talk by Sterl Phinney)

# BH-BH merger

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# BH-BH merger: numerical simulation

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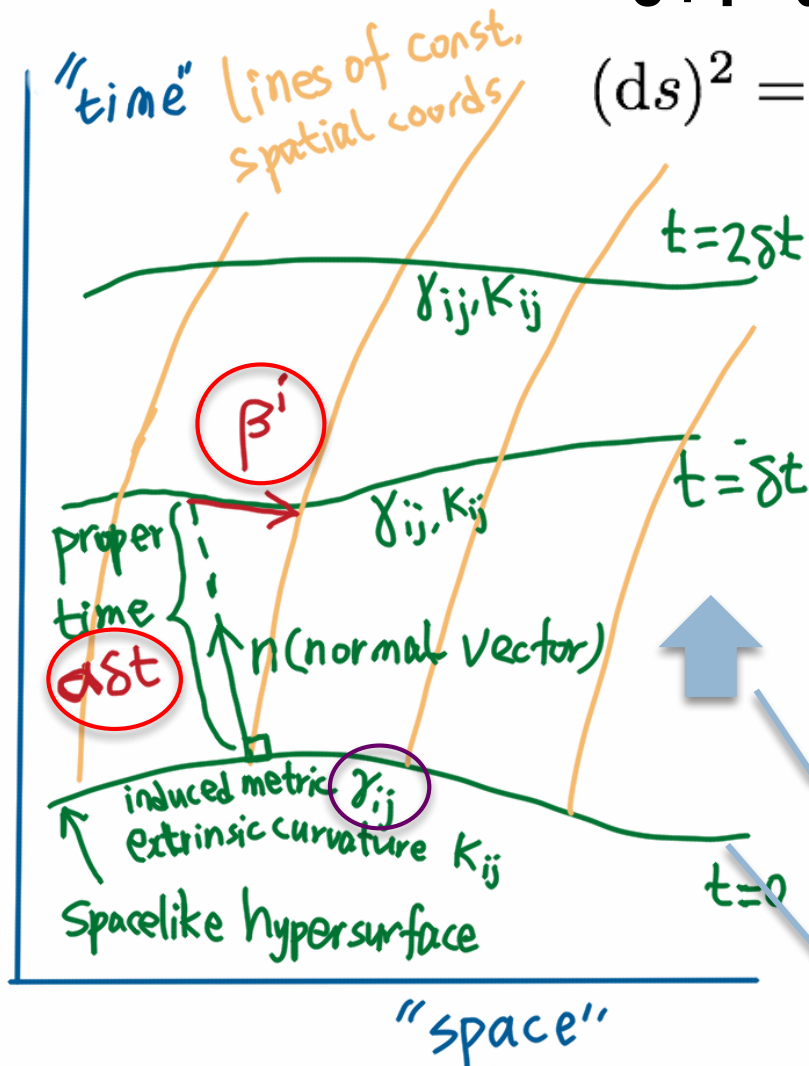
## “3+1” decomposition scheme

$$(ds)^2 = -\alpha^2 dt^2 + \gamma_{ij} (dx^i + \beta^i dt)(dx^j + \beta^j dt)$$

No equations for  $\alpha$  and  $\beta^i$ ! (freedom in choice of coords, **needs a gauge**)

Only 2 **stable** evolution schemes known

- Harmonic coordinates  
(Pretorius 2005, first success)
- Baumgarte-Shapiro-Shibata-Nakamura  
(Baker et. al.; Campanelli et. al., 2006)



Evolution equations  
(hyperbolic)

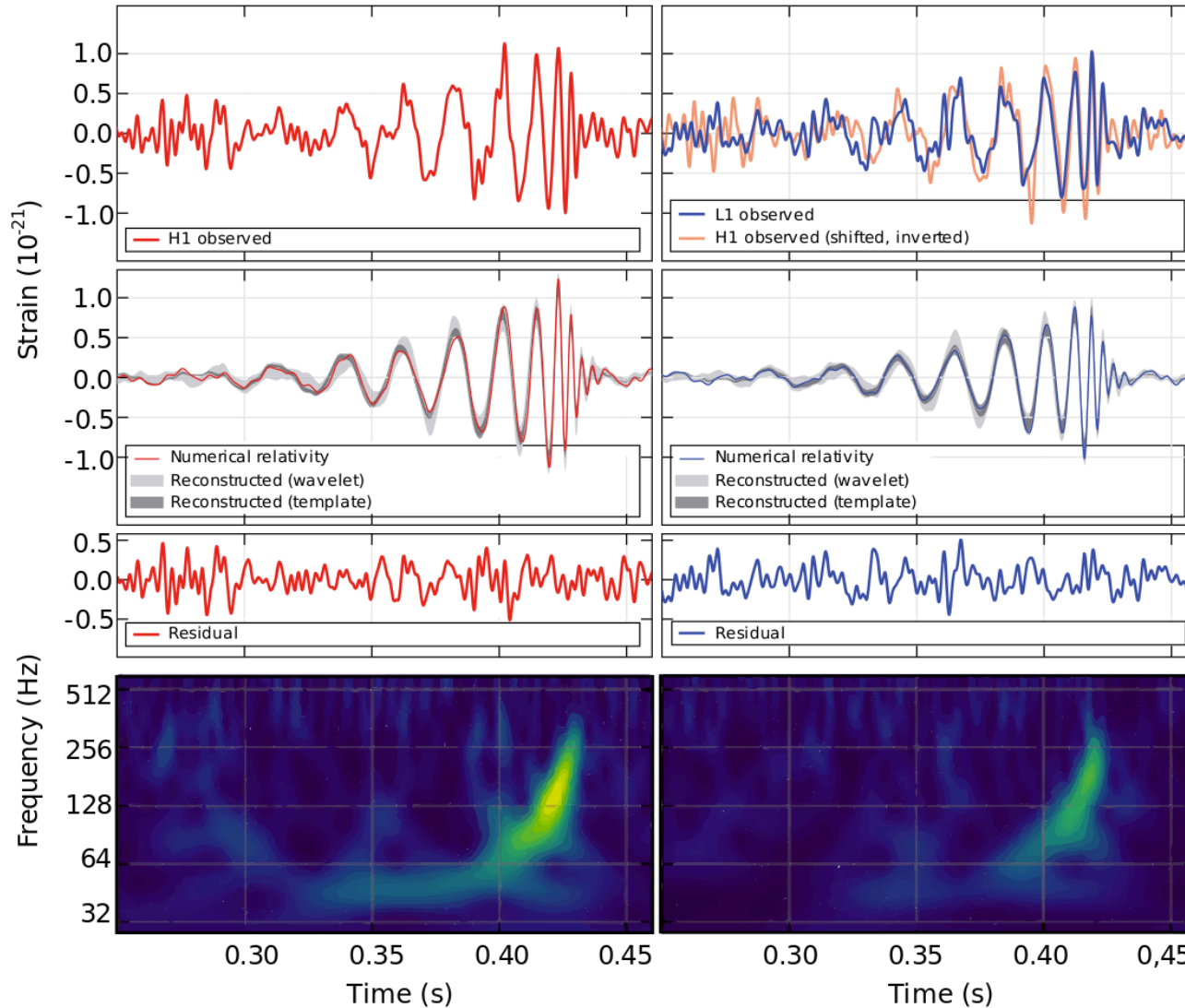
Constraint equations  
(elliptic)

# GW150914: first LIGO detection

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Hanford, Washington (H1)

Livingston, Louisiana (L1)



**14 Sep. 2015**

**Pre-merger: 35+30 solar masses**

**After merger: 62 solar masses, spin 0.68**

**Distance: 440 Mpc**

Abbott et. al.,

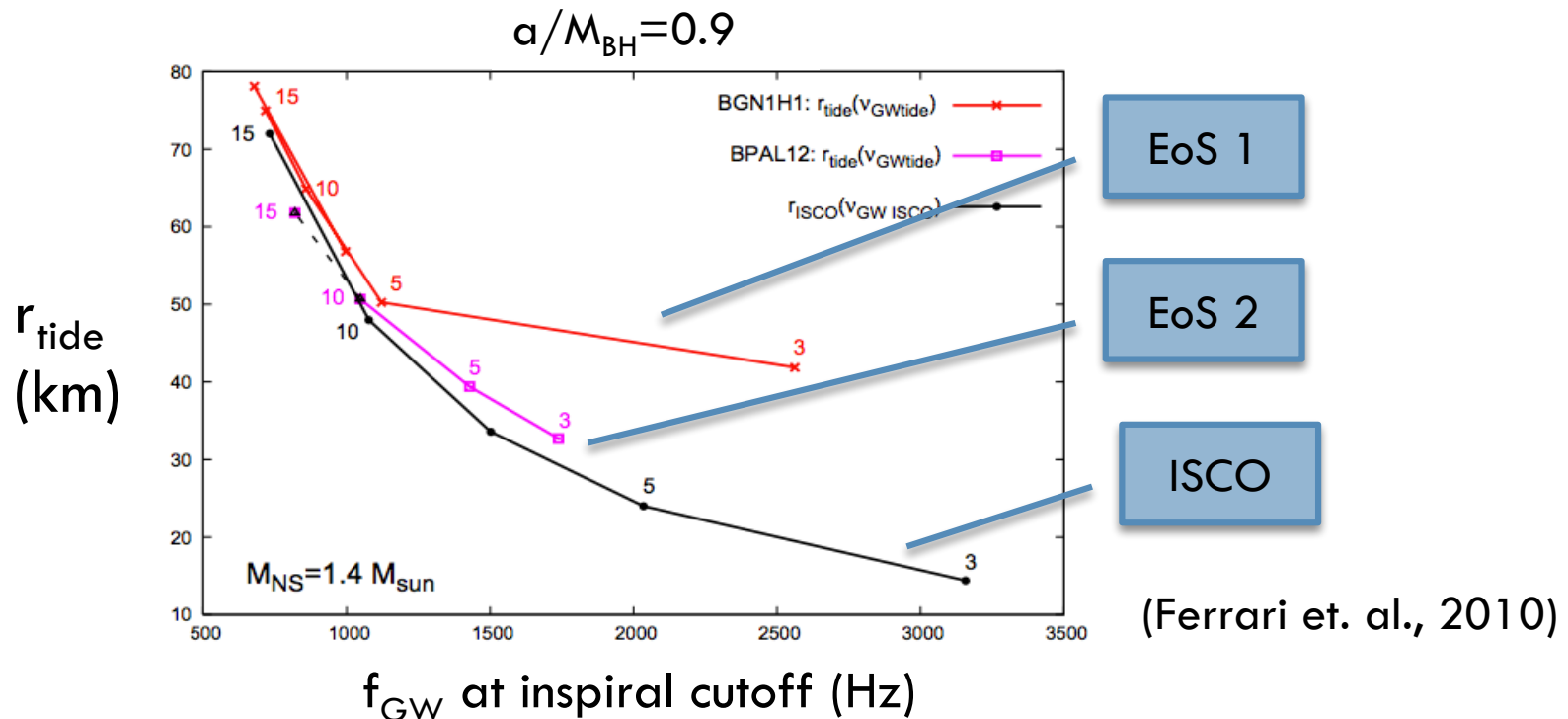
*Phys. Rev. Lett.*

116, 061102 (2016)

# NS-BH tidal disruption

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- Happens when BH tidal field pulls NS apart
- Can tell by inspiral cutoff
- Can be used to probe NS equation of state



- Possibly associated with GRB

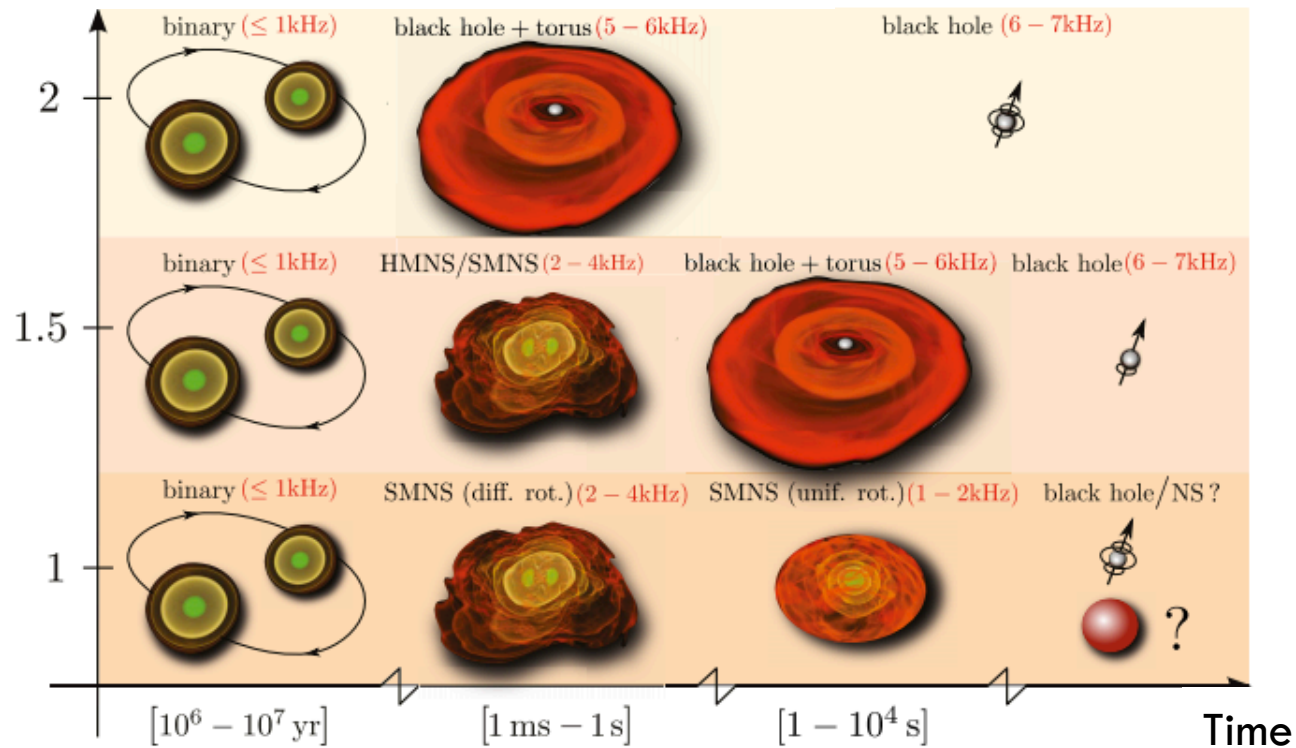


# NS-NS merger

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## NS EoS, GRB association?

$M/M_{\text{TOV}}$  for equal mass binaries

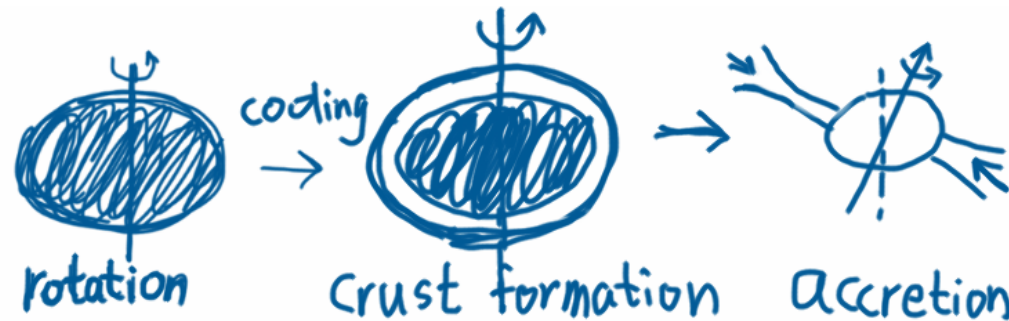


(Baiotti & Rezzolla, 2017)

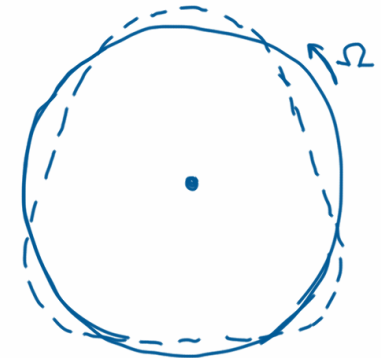
# NS spin & pulsation (in our own galaxy)

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- Emission of GW from **rotation** of solid NS crust



- Emission of GW from NS **pulsation**
  - ▣ Modes damped down by GW and viscosity?
  - ▣ Look for **unstable modes** in fast-rotating NSs
    - Dynamical instabilities (hydrodynamic in origin)
    - Secular instability (driven by dissipation)

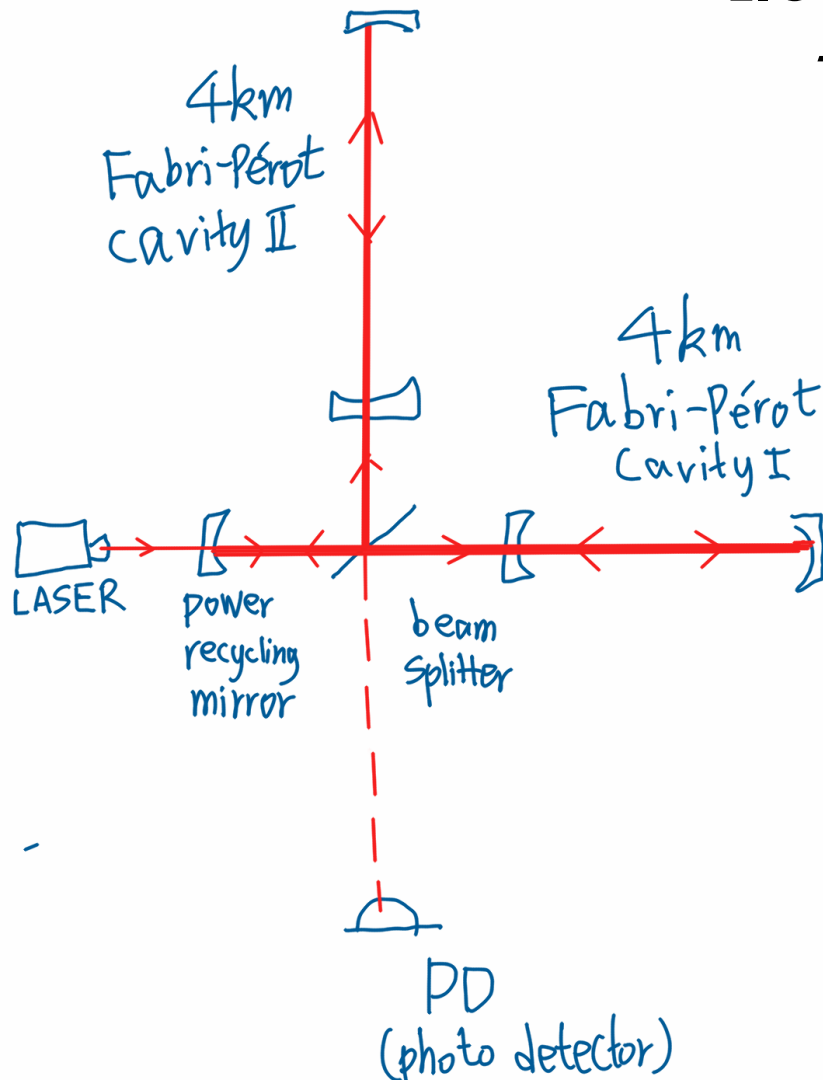


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## Part III. GW detection techniques

# LIGO (Laser Interferometer GW Observatory)

## LIGO's Two key challenges



1. Phase difference:

$$\Delta\Phi = khL = \frac{2\pi}{\lambda_E} hL \sim 10^{-12}$$

10<sup>-22</sup>

4km

10<sup>-4</sup> cm

Solution: use a **Fabri-Pérot cavity** (store light for a time  $\sim T_{\text{GW}}/2$ )

2. The energetic quantum limit:

$$\propto \sqrt{I_0} \quad \Delta E \cdot \Delta t \geq \hbar$$

$\propto \Delta\Phi$

Needs  $I_0 > 100\text{W}$

Solution: use a **power recycling mirror**

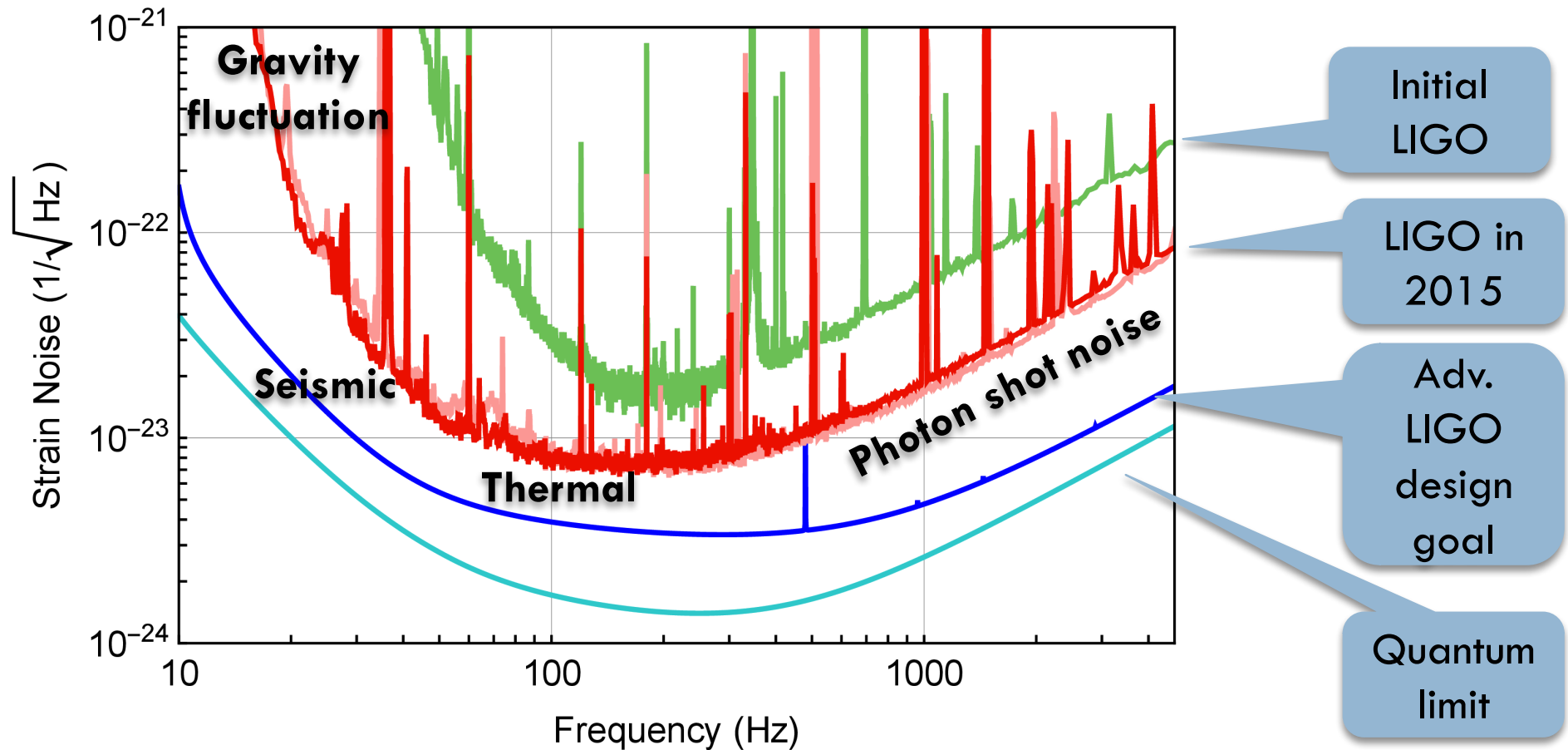
# Everything seems impossible in LIGO

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- Noises, noises, noises!!!
- Noises that affect the **position of the mirror**
  - ▣ Seismic vibrations ( $\sim 10^{-4}$  cm)
  - ▣ Thermal vibrations of the mirror
    - Brownian motion of CM ( $\sim 10^{-10}$  cm)
    - Fluctuation of mirror surface ( $\sim 10^{-14}$  cm)
- Noises that affect the **ability to measure** the position of the mirror
  - ▣ Scattering by residual gas in the vacuum system
  - ▣ Photon shot noise
  - ▣ Radiation pressure

# LIGO sensitivity curve

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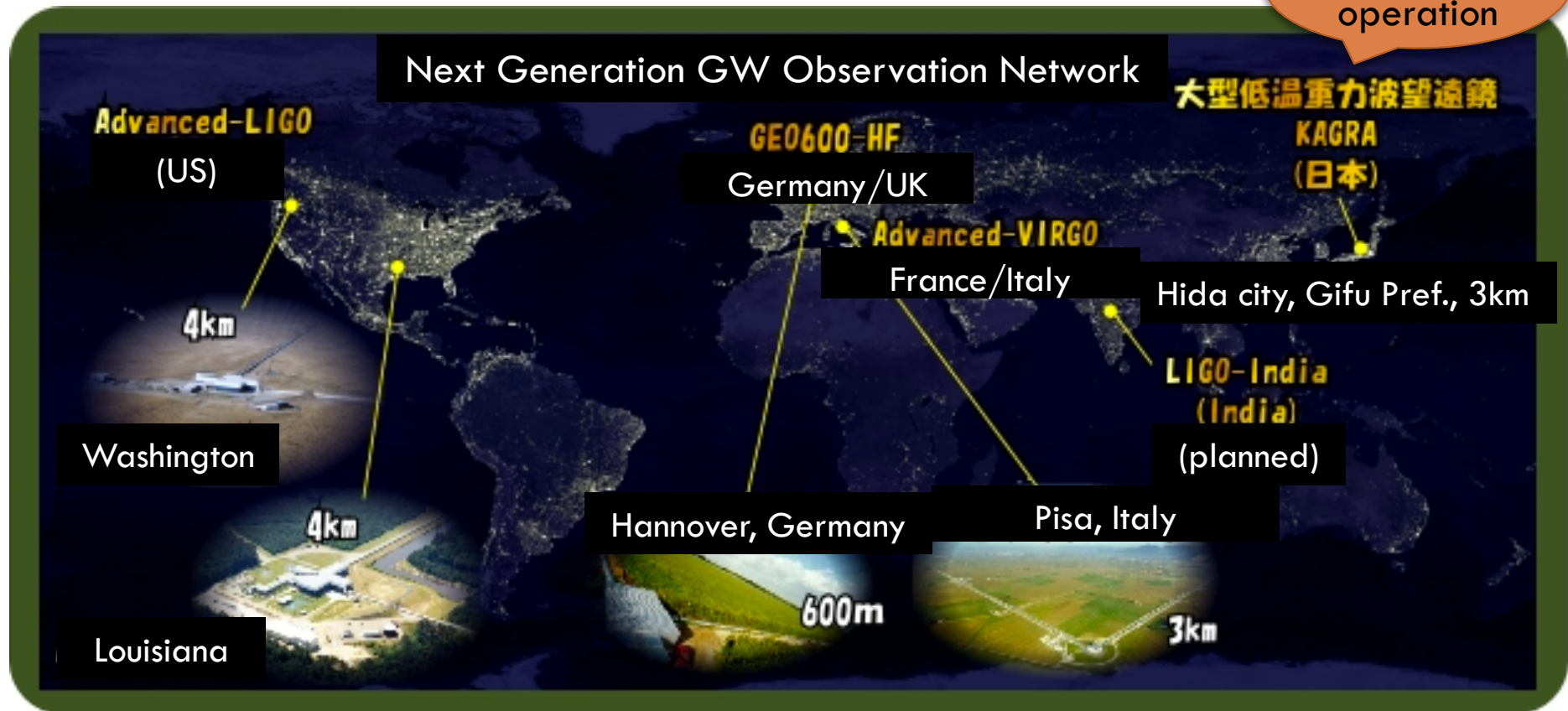


Abbott et. al., *Phys. Rev. Lett.* 116, 131103 (2016)

# LIGO-like projects around the world

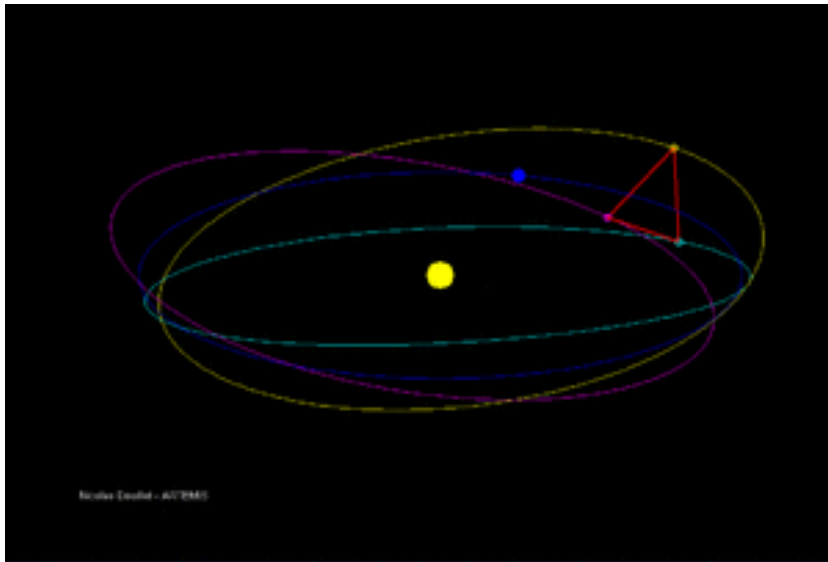
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Cryogenic operation

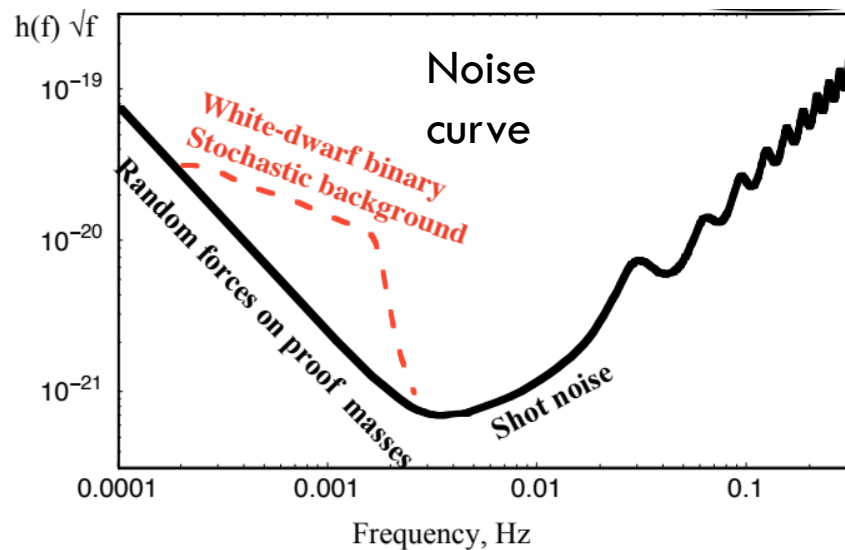


# LISA (Laser Interferometer Space Antenna)

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- LISA is back!! (planned 2034)
  - 3-spacecraft constellation
  - Arm length = 2.5 million km
  - No Fabri-Pérot cavity
  - Much lower frequency band
  - Much lower temperature

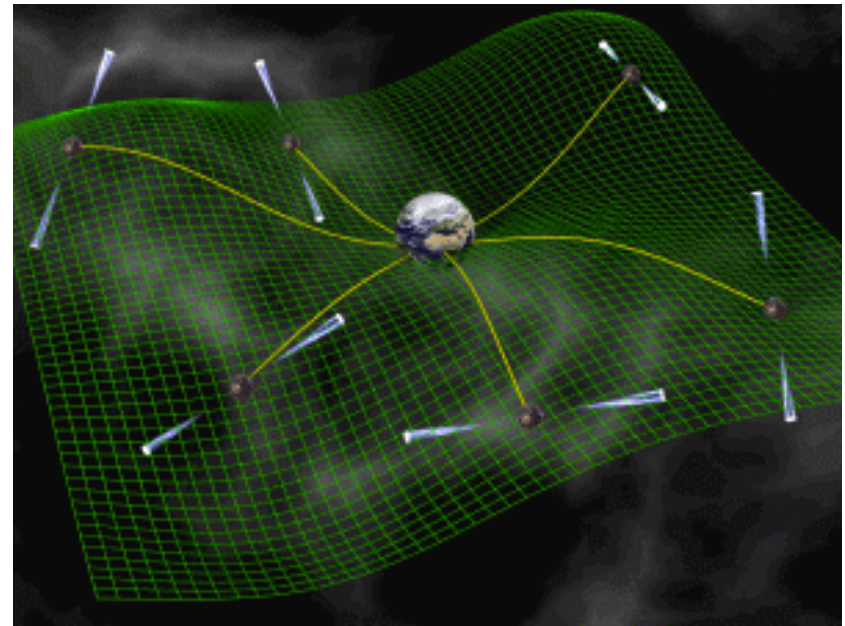




# Pulsar timing

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- GW passing earth can cause **correlated changes** in pulse arrival times
- Suitable for detecting **very low frequency** GWs
  - e.g. SMBH inspiral & merger
- For  $h \sim 10^{-13}$ ,  $T_{\text{GW}} \sim 1 \text{ yr}$ , arrival time change  $\sim 10^{-6} \text{ s}$



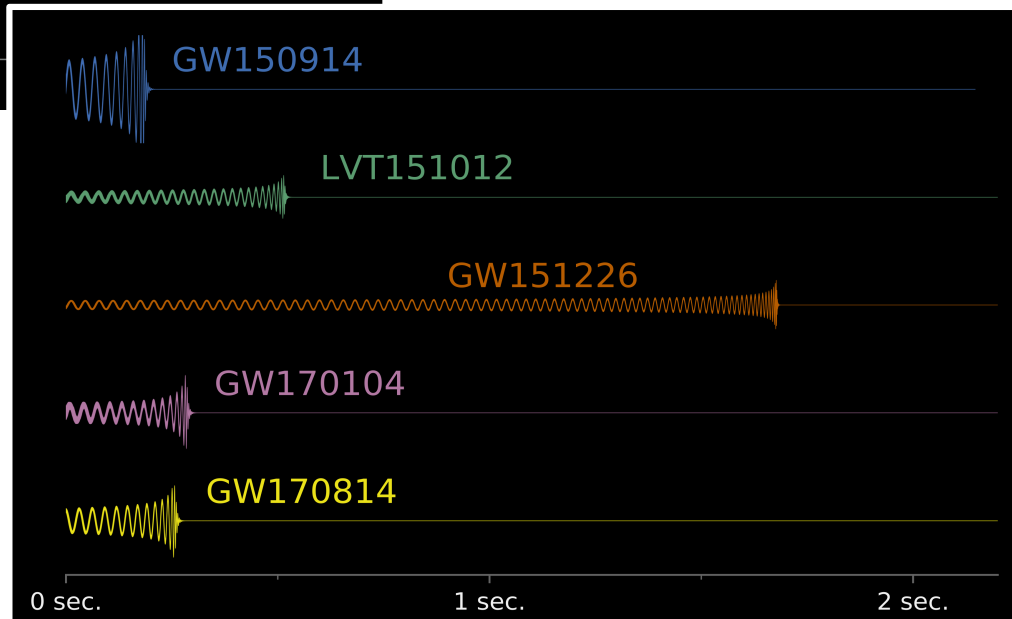
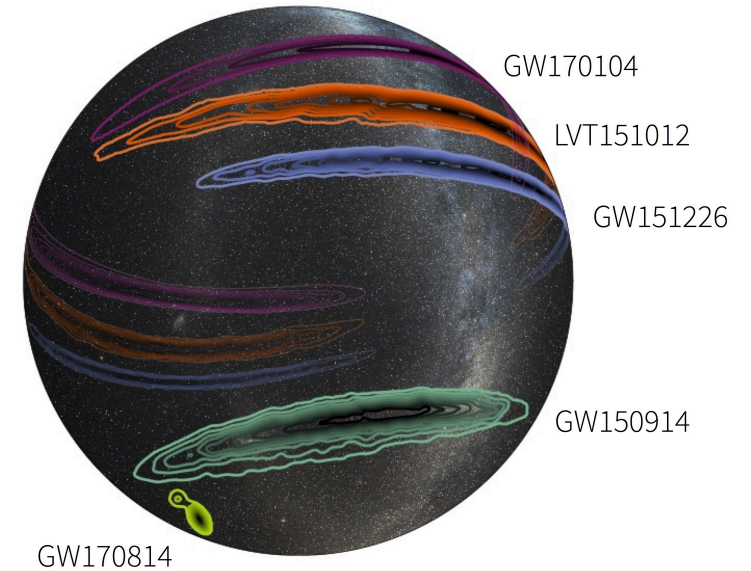
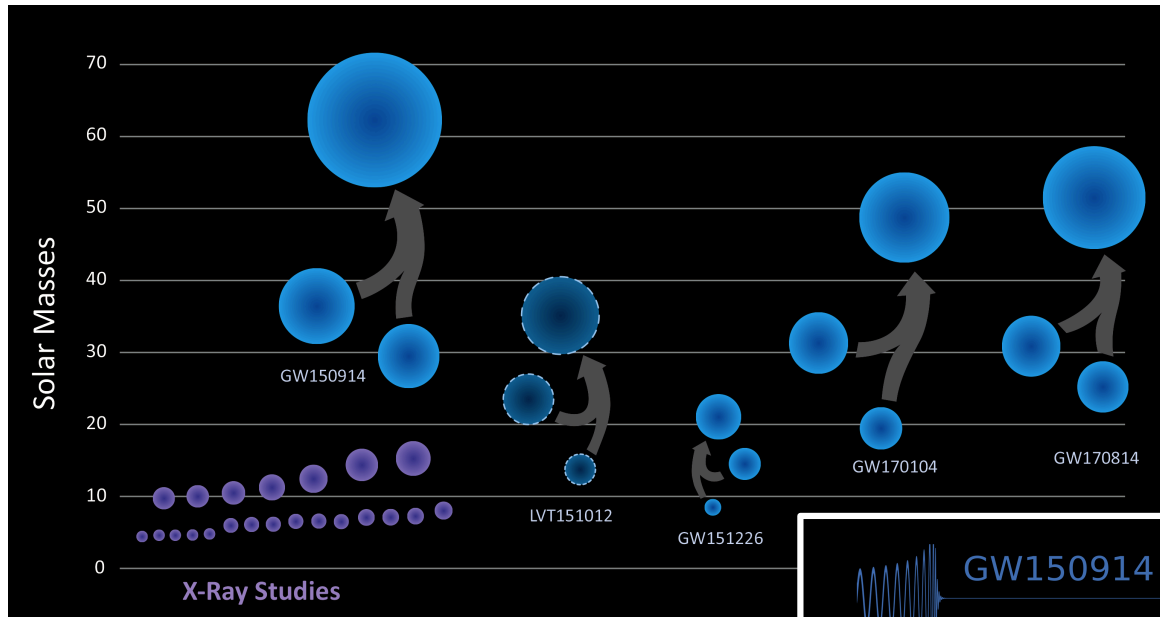
credit: David J. Champion

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## Part IV. LIGO findings

# Up till now: 4 BH-BH merger events

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# GW170817: NS-NS merger?

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- Both LIGO and VIRGO detected a new kind of signal on August 17<sup>th</sup>
  - ▣ Optical counterpart (**SSS17a**) seen from NGC 4993 (40 Mpc away)
  - ▣ Chandra observed **SGRB170817A** from the same position on Aug. 19<sup>th</sup>
  - ▣ If real, first confirmation that short GRB can come from merging neutron stars.



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This is the end. THANK YOU!